

# ON THE EXISTENCE OF EQUILIBRIA IN A CLASS OF BAYESIAN ALLOCATION-MECHANISMS

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ABSTRACT. We study the question of equilibrium-existence in the following class of  $N$ -player Bayesian games. Each player  $n \in \{1, \dots, N\}$  has a general type space  $\Omega_n$ , and there's a prior  $p$  on  $\Omega = \prod_{n=1}^N \Omega_n$  that is absolutely continuous with respect to the product of its marginals. The action space  $A_n$  of player  $n$  is compact Hausdorff. The outcome space, denoted  $\Delta(Z)$ , is the set of probability distributions over a finite set  $Z$ . The outcome function is given by  $\lambda : A \rightarrow \Delta(Z)$ , where  $A = \prod_{n=1}^N A_n$ . Transfers are denoted by  $t_n$  and payoffs by  $u_n : \Omega \times Z \times \mathbb{R} \rightarrow \mathbb{R}$ , so  $u_n(\omega, z, t_n)$  is the payoff to  $n$  when the type profile is  $\omega$ , the outcome is  $z$  and the payment he makes is  $t_n$ . We assume that the game is "mildly discontinuous" in the sense that  $\lambda$  is continuous almost everywhere. The model subsumes standard auction models. We provide sufficient conditions for the existence of Nash equilibria in mixed strategies as well as in pure strategies, and also  $\varepsilon$ -Nash equilibria in these games and explore the implications of these results for auctions.

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