

# Interoperability between Ad-Financed Platforms with Endogenous Multi-Homing

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*\*The views expressed are those of the authors and do not reflect the official position of the European Commission.*

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# Interoperability in digital markets

Networks or systems are *interoperable* if they can “work together”

→ **Horizontal** vs. vertical interoperability

→ Some **common functionalities** can be used across different services

## Digital Markets Act

- Interoperability between **messaging services** (Art. 7)
- Restricted to a few “basic functionalities” (Art. 7.2)
- Applies only to dominant players (“gatekeepers”)

→ WhatsApp and Facebook Messenger designated

Idea that interoperability does not emerge as market outcome, hence the need for regulatory intervention

# This paper

When platforms are **ad-funded** and users can **multi-home**:

- What are the incentives for ad-funded messaging platforms to make their services interoperable?
- How do these incentives compare to the social optimum?
- Symmetric vs. asymmetric platforms?

## Main results:

- Interoperability reduces multi-homing on the consumer side
- When platforms are symmetric, interoperability emerges and is efficient
- If one platform has a large installed base advantage, interoperability does not arise in equilibrium, whereas it would be efficient...
- ... but mandating interoperability may not be efficient in very asymmetric markets.

## Compatibility between networks and possibility of multi-homing

- Katz and Shapiro (1985); Crémer, Rey and Tirole (1999); De Palma, Leruth and Regibeau (1999); Doganoglu and Wright (2006)
- Contributions:
  - Effect of interoperability on equilibrium with endogenous multi-homing
  - Ad-funded business model → effect of interoperability on advertising side

## Multi-purchasing, ad-funded business models and differentiation

- Ambrus and Reisinger (2006); Anderson, Foros and Kind (2016); Athey, Calvano and Gans (2016); Haan, Stoffers and Zwart (2021)
- Contribution:
  - Exposure to advertising depends on the (endogenous) amount of time consumers spend online

# The model

Two horizontally differentiated **messaging platforms**,  $A$  and  $B$

- Symmetric (for the moment)
- Purely ad-funded  $\rightarrow$  no fee for users, but ads are a nuisance
- Charge advertisers a price  $p_i$  per ad
- Decide non-cooperatively on an **interoperability level**  $\phi_i \in [0, 1]$   
 $\rightarrow$  Quality of communications on-net = 1, off-net  $\leq 1$

Mass 1 of **consumers**

- Can single-home on  $A$  or  $B$ , or multi-home  
 $\rightarrow$  Care about how many users to interact with (network effects)
- Decide **how much time** spent communicating on-net and off-net

Mass 1 of homogeneous **advertisers**

- Expected value of exposing users to ads  $\uparrow$  linearly with time spent

1. Platforms non-cooperatively choose their level of interoperability  $\phi_i$   
→ resulting level of interoperability  $\phi = \min\{\phi_A, \phi_B\}$
2. Platforms simultaneously choose their price per ad  $p_i$ , and advertisers decide which platform(s) to buy ad space on
3. Consumers decide which platform(s) to join and how much time they want to spend communicating on-net and off-net

# Time spent online

Consumers decide to **single-home** on platform  $A$  or  $B$ , or **multi-home**

Then, decide **how much time** to spend communicating on-net and off-net:

$$\tau_{on}^* \equiv \operatorname{argmax}_{\tau} u(\tau) - \gamma r_i \tau \quad \text{and} \quad \tau_{off}^* \equiv \operatorname{argmax}_{\tau} \phi u(\tau) - \gamma r_i \tau$$

with  $u(\tau) = \kappa \frac{\tau^{1-\frac{1}{\beta}}}{1-\frac{1}{\beta}}$ , with  $\beta$  elasticity to ad nuisance.

Denoting  $\theta \equiv \phi^\beta$ , we have:

$$\tau_{off}^*(\theta, r_i) = \theta \tau_{on}^*(r_i)$$

and the **net utility** from on-net and off-net coms can be written:

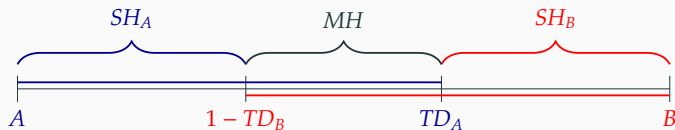
$$\alpha(r_i) \text{ and } \theta \alpha(r_i), \text{ with } \alpha'(\cdot) < 0$$

→ e.g., utility from single-homing on  $i$ :  $v_0 + \alpha(r_i)(n_i + \theta n_j)$

# Interoperability and multi-homing

## Effect of interoperability on multi-homing

An increase in the level of interoperability  $\theta$  *reduces* consumer multi-homing



$$\frac{dTD_A}{d\theta} = \frac{\alpha}{t} \left[ -SH_A + (1 - \theta) \frac{dSH_A}{d\theta} \right] < 0$$

- For given single-homing demands,  $\uparrow$  interoperability improves the quality of off-net coms  $\Rightarrow$  multi-homing *less* attractive
- **Countervailing effect:** single-homing  $\uparrow \Rightarrow$  multi-homing *more* attractive
- The first effect always dominates the second effect



# Equilibrium level of interoperability

## Equilibrium on the advertising market

In equilibrium,  $r_i = 1$  and platforms set advertising price

$$p_i = \sigma \tau^{SH} SH_i + \frac{\sigma \tau_{on}^*}{2} MH \quad \text{with } \tau^{SH} = TD_i \tau_{on}^* + SH_j \tau_{off}^*$$

Then, platforms choose their level of interop. to maximize their profit:

$$\Pi_i(\theta_i, \theta_j) = \sigma \tau^{SH}(\theta) SH_i(\theta) + \frac{\sigma \tau_{on}^*}{2} MH(\theta) \quad \text{with } \theta = \min\{\theta_i, \theta_j\}$$

## Equilibrium level of interoperability

In equilibrium, platforms implement perfect interoperability ( $\theta^* = 1$ )

$\Rightarrow$  Socially-optimum level of interoperability is also  $\theta^w = 1$

# Intuition for the equilibrium outcome

**Platforms' profit** increases with the level of interoperability:

$$\frac{d\Pi_A}{d\theta} = \left( \sigma\tau^{SH}(\theta) - \frac{\sigma\tau_{on}^*}{2} \right) \frac{dSH_A}{d\theta} + \frac{\sigma\tau_{on}^*}{2} \frac{dTD_A}{d\theta} + \sigma \frac{d\tau^{SH}(\theta)}{d\theta} SH_A > 0$$

1. **Market power effect (+)** : Some multi-homers become exclusive users of  $A \rightarrow$  increases market power over advertisers
2. **Total viewership effect (-)** : Less multi-homing  $\rightarrow$  lower total user base to be monetized
3. **Usage intensification effect (+)** :  $\uparrow$  interoperability  $\Rightarrow$  single-homers spend more time communicating on  $A \Rightarrow$  increases exposure to ads and thus ad revenues

**Consumer surplus** increases with the level of interoperability:

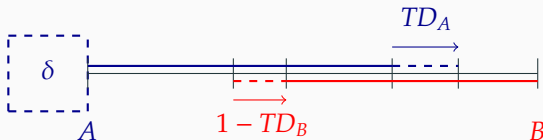
$$\frac{dCS}{d\theta} = 2\alpha SH_A SH_B + \alpha(1 - \theta) \left[ SH_A \frac{dTD_A}{d\theta} - SH_B \frac{dSH_A}{d\theta} \right] > 0$$

- $\uparrow$  quality off-net coms. effect (+)  $>$   $\downarrow$  multi-homing effect (-)

# Platform asymmetry

Assume now that there is a mass  $\delta > 0$  of users located at 0

- Will always choose to single-home on A  $\rightarrow$  *installed base* of A



A larger **installed base** makes platform A...

- More attractive to users in the “competitive” segment
- More attractive to advertisers: it can charge higher ad prices

Higher **interoperability** levels the playing field...

- In terms of total user demand
- In terms of ad prices

# Equilibrium level of interoperability with asymmetry

## Platforms' interoperability choices

- The small platform always prefers **perfect interoperability**
- The large platform prefers **no interoperability** if the installed base is large enough ( $\delta > \delta_{\Pi_A}$ ), and **perfect interoperability** otherwise ( $\delta \leq \delta_{\Pi_A}$ )

**Intuition:**  $B$  **benefits** more and is **hurt** less by interoperability than  $A$ .

- **Market power effect: (+) for  $B$ , (-/+ ) for  $A \rightarrow p^{SH} - p^{MH}$**  higher for  $B$  than for  $A$ ; and stronger increase in  $SH_B$  than  $SH_A$  (which can decrease for low  $\theta$ ).
- **Total viewership effect: (+/-) for  $B$ , (-) for  $A \rightarrow p_A^{MH} > p_B^{MH}$**  and stronger decrease in  $TD_A$  than  $TD_B$  (which can increase for low  $\theta$ ).
- **Usage intensification effect: (+) for  $B$ , (-/+ ) for  $A \rightarrow$**  Increase in time spent on  $B$ , reflected in higher ad price for  $B$ , lower for  $A$ .

# Comparison with social optimum with asymmetry

## Comparison with social optimum

The equilibrium level of interoperability is weakly too low from a welfare point of view

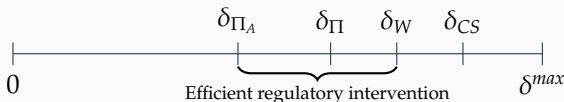
### Intuition:

Consumer surplus is maximized with full interoperability if  $\delta < \delta_{CS}$ , and no interoperability otherwise. This is because high  $\delta$ :

- reduces volume of off-net interactions, weakening the  $\uparrow$  quality off-net interactions effect (+).
- induces stronger shifts towards market single-homing (-).

Advertiser surplus always fully extracted by platforms.

Therefore, we have:



# Conclusion

## Interoperability...

- Increases the market power of platforms over advertisers
- Stimulates the engagement of single-homers due to higher quality interactions, increasing their exposure to advertising
- Reduces the total viewership that the platforms can monetize on the advertiser side

**Symmetric platforms:** positive effects outweigh negative effect, and perfect interoperability emerges w/o regulatory intervention

**Asymmetric platforms:** negative effect may outweigh positive effects for large platforms → interop. doesn't emerge w/o intervention

## Policy implications:

- interoperability may increase the market power of platforms in the advertising market
- mandating interop. may not be efficient in very asymmetric mkts

Thank you for your attention!

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