

# Is a market-based approach to climate policy desirable?

**Felix Bierbrauer**  
**University of Cologne**

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# The market-based approach

- Climate policy goals should be reached with a uniform price on CO<sub>2</sub> emissions. With a “correct” price, emission reductions are realized with minimal costs to society. Sector-specific rules are superfluous or even harmful.
- The market-based approach provides “correct” incentives for firms confronted with switching to greener technologies or paying for emissions. No need for the government to provide further incentives for the use of green technologies.

**Political reality:** Sector-specific rules all over the place

- European Union: emission trading system covering e.g. electricity and heat generation, aluminium, cement, steel works... Separate emission trading system (EU ETS II) planned covering buildings and road transport, CO<sub>2</sub> emission performance standards for cars and vans.
- Germany: Green taxes covering fossil fuels and electricity, regulation of heating systems.

# Main results

## Is there a plausible justification for a sector-specific approach?

- 1 There are somewhat restrictive conditions under which the market-based approach is justified in the sense that any departure from it implies a violation of Pareto-efficiency.
- 2 More generally the market-based approach can be justified under an assumption of *distributive indifference* and with *proportional fiscal externalities*.
- 3 In the presence of a non-linear income tax, sector specific policies can be justifiable even under *distributive indifference*.
- 4 With distributive concerns, sector specific rules and hence a departure from the market-based approach can be justified.

## Related literatures

- Regulation of externalities: Weitzman (1974), ... partial equilibrium model
- Sector-specific taxation: Ramsey (1927), Diamond and Mirrless (1971), Diamond (1975),...
- General equilibrium tax incidence: Harberger (1962), Bovenberg and Goulder (1994), Tsyvinki et al. (2020) ...
- Direct versus indirect taxation: Atkinson-Stiglitz (1976), Saez (2002), Hellwig and Werquin (2023)
- Optimal externalities and optimal taxation: Cremer, Gahvari and Ladoux (1998), Golosov et al. (2014), Jacobs and de Mooij (2015), Jacobs and van der Ploeg (2019), Pai and Strack (2022) and Ahlvik et al. (2024).
- Distributive consequences of carbon pricing: Känzig (2023)

# Households I

- Unit mass of households with preferences  $u(x_c, \chi(\beta x_g, x_b)) - k(y, \omega)$ .
- Consumption utility  $u$  assumed to be homothetic

$x_c$ : unspecific consumption good

$\chi$ : subutility from combining a green ( $x_g$ ) and a brown ( $x_b$ ) good.

$\beta$ : strength of the preference for the green vs the brown good.

- Effort cost function  $k$

$y$ : labour supply in efficiency units,

$\omega$ : productive ability, affects the marginal effort costs,  $k_{12} < 0$ .

- Budget constraint:

$$q_c x_c + q_g x_g + q_b x_b \leq p_w y_l - T_l(p_w y_l) + s \Pi^E + \mathcal{R}^E, \quad (1)$$

where  $q_j = (1 + t_j)p_j$ , for  $j \in \{c, g, b\}$ .

# Households II

Implications:

- Engel curves are linear. Heterogeneity in the composition of the consumption basket only due to heterogeneity in the preference for green versus brown consumption goods, parameterized by  $\beta$ .
- A hypothetical redistribution of one unit of income from a high  $\beta$  to a low  $\beta$  person reduces the demand for emission intensive goods.

For some of the results impose **Assumption 1**:

- $u(x_c, \chi(\beta x_g, x_b)) = x_c^{1-\nu} \chi(\beta x_g, x_b)^\nu$
- $\chi = \left( \beta x_g^{1-\varepsilon_\chi} + x_b^{1-\varepsilon_\chi} \right)^{\frac{1}{1-\varepsilon_\chi}}$ .
- $\nu$  small.

Think of the green and the brown sector as targets for specific policies vis à vis *the rest of the economy*.

# Firms I

The profit-maximization problem of a generic firm in sector  $j \in \{c, b, g\}$  is to choose labour demand  $l$  and  $R\&D$  effort  $r$  to maximize

$$p_j \alpha f_j(l) - p_w l - t_{je} (e_{j0} - a_j(r)) \alpha f_j(l) - p_c \gamma r .$$

- The abatement function  $a_j : r \mapsto a_j(r)$ , with  $a_j(0) = 0$ , gives the decrease in the emission intensity of production.
- The production function  $f_j$  is assumed to satisfy the usual Inada conditions.
- Firms differ in factor productivity  $\alpha$  and abatement costs  $\gamma$ .
- There are, possibly sector-specific, taxes/ prices for emission permits  $t_{je}$ .

## Firms II

### Lemma

Consider a firm in sector  $j \in \{c, b, g\}$  with characteristics  $\theta_j = (\alpha_j, \gamma_j)$ . Let  $f_j$  be iso-elastic. Then the firm's choices  $y_j^*$ ,  $l_j^*$ ,  $r_j^*$  and  $e_j^*$  are all increasing in  $p_j$  and decreasing in  $p_w$ ,  $t_{je}$ . For  $j \in \{b, g\}$  they are decreasing in  $p_c$ .

Implications:

- Reducing emissions relative to a status quo necessarily goes together with lower output, employment and abatement.
- Abatement can mitigate but not offset this effect. Complementarity of labor demand and abatement effort:
  - Treating  $r$  as a parameter,  $l^*$  increases in  $r$ .
  - Treating  $l$  as a parameter,  $r^*$  increases in  $l$ .



# Competitive equilibrium given policy I

Policy  $\mathcal{T}$  consists of

- Consumption taxes  $t_x = (t_c, t_g, t_b)$ .
- Emission taxes  $t_e = (t_{ce}, t_{ge}, t_{be})$ .
- A possibly non-linear labor income tax  $T_l : p_w y_l \mapsto T_l(p_w y_l)$ .

Equilibrium prices for labour,  $p_w^*$ , and consumption goods ensure market clearing.

- For consumers denoted by  $q_c^*, q_g^*, q_b^*$ .
- For producers denoted by  $p_c^*, p_g^*, p_b^*$ .

## Proposition 1 (Existence and uniqueness)

Under Assumption 1, there is a unique equilibrium price vector.

- Lemma: Walras's Law holds, can set  $p_w = 1$ .

# Competitive equilibrium given policy II

## Proposition 2 (Tax incidence)

Under Assumption 1:

- 1  $t_c \uparrow \Rightarrow p_c \downarrow, q_c \uparrow.$
- 2  $t_{ce} \uparrow \Rightarrow p_c, q_c \uparrow.$
- 3  $t_{ge} \uparrow$  or  $t_{be} \uparrow \Rightarrow p_g, q_g, p_b, q_b \uparrow.$
- 4  $t_b \uparrow \Rightarrow p_b \downarrow, p_g, q_g, q_b \uparrow.$
- 5  $t_g \uparrow \Rightarrow p_g \downarrow, q_g, p_b, q_b \uparrow.$

## Proposition 3 (More socially responsible consumers)

Under Assumption 1, when “ $\beta$  increases”, then:

- 1  $p_g, q_g \uparrow.$
- 2  $p_b, q_b \downarrow.$

Consequence: the green sector becomes greener, the brown sector browner.

## A first best benchmark I

Let there be a given utility profile  $U_0 : \theta \mapsto U_0(\theta)$ . We say that an allocation is first best if it is physically feasible and **reaches this utility profile with minimal emissions**.

### Proposition 4 (First-best benchmark)

At a solution to a first-best problem:

- i) The marginal costs of abatement are equalized across firms and sectors.
- ii) The marginal rates of substitution between any pair of consumption goods are equalized across households.
- iii) The marginal rates of substitution between consumption goods and effort costs are equalized across households.

**Corollary:** With sector specific CO2 prices, differential commodity taxation or non-linear income taxation, a competitive equilibrium allocation is not first best.

**But:** First best allocations are typically not incentive-compatible. And those that are have distributive implications which may be problematic.

## A second-best benchmark I

**Assumption AS (Atkinson-Stiglitz, 1976):**  $\beta$  is the same for all;  $s$  is the same for all.  $\Rightarrow$  Individuals differ only in  $\omega$ .

**Second-best problem:** Add an incentive compatibility constraint to the first-best problem. For any pair  $\omega, \omega', U_0(\omega) \geq u_0(\omega') - k(y_l(\omega'), \omega)$ .

### Proposition 5 (Heterogeneity only in productive abilities)

Under Assumption AS, at a solution to a second-best problem:

- i) The marginal costs of abatement are equalized across firms and across sectors.
- ii) The marginal rates of substitution between any pair of consumption goods are equalized across households.

**Corollary:** With sector specific CO2 prices or differential commodity taxation a competitive equilibrium allocation is not second-best. Non-linear income taxation is no impediment for reaching a second-best outcome.

**But:** Assumption AS is interesting as a benchmark, not empirically plausible.

# The market-based approach: A good idea? I

**The emission target.** We assume that there is a national emission target  $\bar{\mathcal{E}}$ :

$$\mathcal{E}(p^*(\mathcal{T}), t_e) \leq \bar{\mathcal{E}}. \quad (2)$$

where

$$\mathcal{E}(p^*(\mathcal{T}), t_e) := \sum_{j \in \{c, g, b\}} \mathbf{E}_j[\mathbf{e}_j^*(p^*(\mathcal{T}), t_{je}, \theta_j)]$$

# The market-based approach: A good idea? II

Measures of social welfare.

$$\mathcal{W} = \mathbf{E}_{\theta}[g(\theta) U(\theta)] .$$

Shorthands for later use:

- Social marginal utility of disposable income for type  $\theta$ :

$$\mathbf{g}(\tilde{v}(\beta, q_x), \theta) := g(\theta) \tilde{v}(\beta, q) ,$$

where  $\tilde{v}(\beta, q)$  is the marginal utility of disposable income.

- Population average of the social marginal utility of income  $\bar{\mathbf{g}}$ .
- Average amongst recipients of “capital income” from sector  $j$ :  $\bar{\mathbf{g}}_{\Pi j}$ .

## The market-based approach: A good idea? III

**The thought experiment.** Start from an allocation induced by a competitive equilibrium with a market-based approach. Then consider departures from uniform emission taxes and/ or uniform commodity taxes that respect the emission target.

Formally, let  $\tau_1 \in \{t_c, t_g, t_b, t_{ce}, t_{ge}, t_{be}\}$  and  $\tau_2 \in \{t_c, t_g, t_b, t_{ce}, t_{ge}, t_{be}\}$  be two different tax rates. A policy change that respects the emission target needs to satisfy

$$\mathcal{E}_{\tau_1} d\tau_1 + \mathcal{E}_{\tau_2} d\tau_2 = 0$$

or

$$\frac{d\tau_2}{d\tau_1} = -\frac{\mathcal{E}_{\tau_1}}{\mathcal{E}_{\tau_2}}.$$

Let  $d\tau_1 > 0$  and  $d\tau_2 < 0$ . The welfare-implications of such a policy change are positive if

$$\mathcal{W}_{\tau_1} - \mathcal{W}_{\tau_2} \left( \frac{\mathcal{E}_{\tau_1}}{\mathcal{E}_{\tau_2}} \right) > 0.$$

# Welfare implications of policy changes I

## Proposition 6 (Sufficient statistics formula)

Let  $\tau \in \{t_c, t_b, t_g, t_{ce}, t_{be}, t_{ge}\}$ .

$$\begin{aligned}\mathcal{W}_\tau &= -\sum_j \frac{dq_j^*(\mathcal{T})}{d\tau} \text{Cov}(\mathbf{g}(\tilde{v}(\cdot), \theta), x_j^*(\cdot)) \\ &\quad + \bar{\mathbf{g}} \sum_j (q_j^*(\mathcal{T}) - p_j^*(\mathcal{T})) \frac{dX_j^*(\cdot)}{d\tau} \\ &\quad + \frac{dp_c^*(\mathcal{T})}{d\tau_j} \left( (\bar{\mathbf{g}}_{\Pi_c} - \bar{\mathbf{g}}) Y_c^*(\cdot) - \sum_j (\bar{\mathbf{g}}_{\Pi_j} - \bar{\mathbf{g}}) \mathbf{E}_j[\gamma_j r_j^*(\cdot)] \right) \\ &\quad + \frac{dp_g^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_g} - \bar{\mathbf{g}}) X_g^*(\cdot) + \frac{dp_b^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_b} - \bar{\mathbf{g}}) X_b^*(\cdot) \\ &\quad + \bar{\mathbf{g}} \mathbf{E}_\theta [T'_l(y_l^*(\cdot)) y_{l\tau}^*(\cdot)] \\ &\quad + \bar{\mathbf{g}} \sum_j t_{je} \frac{d\mathcal{E}_j^*(\cdot)}{d\tau} \\ &\quad + \sum_j \mathbf{I}(\tau = \tau_{je}) (\bar{\mathbf{g}} - \bar{\mathbf{g}}_{\Pi_j}) \mathcal{E}_j^*(\cdot)\end{aligned}$$



## Welfare implications of policy changes II

**Equity:** Distributive effects across different households

$$\begin{aligned}
 \mathcal{W}_\tau &= - \sum_j \frac{dq_j^*(\mathcal{T})}{d\tau} \text{Cov}(\mathbf{g}(\tilde{v}(\cdot), \theta), x_j^*(\cdot)) \\
 &+ \bar{\mathbf{g}} \sum_j (q_j^*(\mathcal{T}) - p_j^*(\mathcal{T})) \frac{dX_j^*(\cdot)}{d\tau} \\
 &+ \frac{dp_c^*(\mathcal{T})}{d\tau_j} \left( (\bar{\mathbf{g}}_{\Pi_c} - \bar{\mathbf{g}}) Y_c^*(\cdot) - \sum_j (\bar{\mathbf{g}}_{\Pi_j} - \bar{\mathbf{g}}) \mathbf{E}_j[\gamma_j r_j^*(\cdot)] \right) \\
 &+ \frac{dp_g^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_g} - \bar{\mathbf{g}}) X_g^*(\cdot) + \frac{dp_b^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_b} - \bar{\mathbf{g}}) X_b^*(\cdot) \\
 &+ \bar{\mathbf{g}} \mathbf{E}_\theta [T_l'(y^*(\cdot)) y_{l\tau}^*(\cdot)] \\
 &+ \bar{\mathbf{g}} \sum_j t_{je} \frac{d\mathcal{E}_j^*(\cdot)}{d\tau} \\
 &+ \sum_j \mathbf{I}(\tau = \tau_{je}) (\bar{\mathbf{g}} - \bar{\mathbf{g}}_{\Pi_j}) \mathcal{E}_j^*(\cdot)
 \end{aligned}$$

# Welfare implications of policy changes III

**Efficiency:** Change of equilibrium quantities – Behavioral responses

$$\begin{aligned}
 \mathcal{W}_\tau &= - \sum_j \frac{dq_j^*(\mathcal{T})}{d\tau} \text{Cov}(\mathbf{g}(\tilde{v}(\cdot), \theta), x_j^*(\cdot)) \\
 &+ \bar{\mathbf{g}} \sum_j (q_j^*(\mathcal{T}) - p_j^*(\mathcal{T})) \frac{dX_j^*(\cdot)}{d\tau} \\
 &+ \frac{dp_c^*(\mathcal{T})}{d\tau_j} \left( (\bar{\mathbf{g}}_{\Pi_c} - \bar{\mathbf{g}}) Y_c^*(\cdot) - \sum_j (\bar{\mathbf{g}}_{\Pi_j} - \bar{\mathbf{g}}) \mathbf{E}_j[\gamma_j r_j^*(\cdot)] \right) \\
 &+ \frac{dp_g^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_g} - \bar{\mathbf{g}}) X_g^*(\cdot) + \frac{dp_b^*(\mathcal{T})}{d\tau_j} (\bar{\mathbf{g}}_{\Pi_b} - \bar{\mathbf{g}}) X_b^*(\cdot) \\
 &+ \bar{\mathbf{g}} \mathbf{E}_\theta [T'_l(y^*(\cdot)) y_{l\tau}^*(\cdot)] \\
 &+ \bar{\mathbf{g}} \sum_j t_{je} \frac{d\mathcal{E}_j^*(\cdot)}{d\tau} \\
 &+ \sum_j \mathbf{I}(\tau = \tau_{je}) (\bar{\mathbf{g}} - \bar{\mathbf{g}}_{\Pi_j}) \mathcal{E}_j^*(\cdot)
 \end{aligned}$$

# Departing from the market-based approach I

- Uniform commodity taxation in the status quo:

$$\bar{g} \sum_j (q_j^*(\mathcal{T}) - p_j^*(\mathcal{T})) \frac{dX_j^*(\cdot)}{d\tau} = 0.$$

- Uniform CO2 price in the status quo: Let  $t_{je} = \bar{t}_e$ , for all  $j$ .
- **Distributive indifference:** For all  $\theta$ ,  $\mathbf{g}(\tilde{v}(\cdot), \theta) = \bar{\mathbf{g}}$ .
- **Proportional fiscal externalities:** There is a number  $\eta$ , so that, for all  $\tau \in \{t_c, t_b, t_g, t_{ce}, t_{be}, t_{ge}\}$ ,

$$\frac{\mathbf{E}_\theta [T'_l(y_l^*(\cdot, \theta)) y_{l\tau}^*(\cdot, \theta)]}{\mathcal{E}_\tau} = \eta,$$

Under these assumptions

$$\mathcal{W}_\tau = \bar{\mathbf{g}} (\bar{t}_e + \eta) \mathcal{E}_\tau.$$

## Departing from the market-based approach II

**Apply test for the desirability of the market-based approach:** With  $\mathcal{W}_\tau = \bar{g} (\bar{t}_e + \eta) \mathcal{E}_\tau$  have

$$\mathcal{W}_{\tau_1} - \mathcal{W}_{\tau_2} \left( \frac{\mathcal{E}_{\tau_1}}{\mathcal{E}_{\tau_2}} \right) = 0 .$$

Hence, no welfare-gain from departing from the market-based approach.

### Proposition 7 (Suff. conditions for the market-based approach)

Consider a competitive equilibrium induced by a market-based approach to climate policy. With distributive indifference and proportional fiscal externalities there are no welfare gains from deviating from the market-based approach.

# Departing from the market-based approach III

- 1 Is the assumption of distributive indifference normatively appealing?

Suppose that  $s$  or  $\beta$  and  $\omega$  are positively correlated. Then it is incompatible with weights that are higher for people with lower disposable income.

- 2 Is the assumption of proportional fiscal externalities empirically plausible ?

Broadly, what has a small impact on earnings incentives also has a small impact on overall emissions.

Counterexamples are conceivable: E.g. limited  $GE$  effects of taxes on prices, zero emissions for the green good  $\Rightarrow$  tax the green good more than the brown good.

# Can the market-based approach be desirable under alternative assumptions?

- Write  $\mathcal{W}_\tau = \mathcal{W}_\tau^{net} + \bar{g} \sum_j t_{je} \frac{d\mathcal{E}_j^*(\cdot)}{d\tau}$
- Then, starting from the market-based approach, the welfare impact of raising some tax rate  $\tau_1$  and lowering some tax rate  $\tau_2$  is given by

$$\mathcal{W}_{\tau_1}^{net} - \mathcal{W}_{\tau_2}^{net} \left( \frac{\mathcal{E}_{\tau_1}}{\mathcal{E}_{\tau_2}} \right) .$$

It is possible that this expression is (close to) zero even if  $\mathcal{W}_{\tau_1}^{net} \neq 0$  and  $\mathcal{W}_{\tau_2}^{net} \neq 0$ .

- An empirical application of the sufficient statistics approach would tell.
- Question of welfare weights and elasticities – as opposed to principles of climate policy design.

# Equity considerations I

Approach:

- Consider welfare weights that are monotonic in disposable income.
- Again, we consider the equ. that results with  $t_{ce} = t_{be} = t_{ge} =: \bar{t}_e$ , and  $t_c = t_b = t_g = 0$ . Again, check whether, for any pair  $\tau_1, \tau_2$ ,

$$\mathcal{W}_{\tau_1}^{net} - \mathcal{W}_{\tau_2}^{net} \left( \frac{\mathcal{E}_{\tau_1}}{\mathcal{E}_{\tau_2}} \right) = 0, \quad (3)$$

- Special case of the more general model developed in Section 2. Firms operate with constant returns to scale technologies and fixed emission intensities.
  - ⇒ Producer prices are fixed  $p_j = 1 + t_{je} e_{j0}$ .
  - ⇒ Tax increases fully passed to consumers,  $q_j = (1 + t_j)(1 + t_{je} e_{j0})$ .

## Equity considerations II

### Proposition 8 (Rich vs Poor rather than Brown vs Green I)

Consider the competitive equilibrium allocation that results under a market-based approach to climate policy and suppose that fiscal externalities are proportional. Consider two goods  $j, k \in \{c, g, b\}$  so that

$$\text{Cov}(\mathbf{g}(\cdot), x_k^*(\cdot)) < 0 < \text{Cov}(\mathbf{g}(\cdot), x_j^*(\cdot)) .$$

Welfare goes up if public policy deviates from the market based approach when  $t_{ke}$  or  $t_k$  is increased and  $t_{je}$  or  $t_j$  is decreased.



## Equity considerations III

### Proposition 9 (Rich vs Poor rather than Brown vs Green II)

Suppose Assumption 1 holds

- 1 If  $\mathcal{W}_\tau^{net} = 0$  for  $\tau \in \{t_c, t_{ce}\}$ . Let  $\text{Cov}(\mathbf{g}(\cdot), x_j^*(\cdot)) < \text{Cov}(\mathbf{g}(\cdot), x_c^*(\cdot))$ . Then  $\mathcal{W}_\tau^{net} > 0$  for  $\tau \in \{t_j, t_{je}\}$  and  $\mathcal{W}_\tau^{net} < 0$  for  $\tau \in \{t_{-j}, t_{-je}\}$ .
- 2 Suppose that for all individuals  $\beta$  takes the same value, henceforth denoted by  $\bar{\beta}$ . Then, for any pair  $\tau_1, \tau_2 \in \{t_{ce}, t_{ge}, t_{be}, t_c, t_g, t_b\}$

$$\text{sgn } \mathcal{W}_{\tau_1}^{net} = \text{sgn } \mathcal{W}_{\tau_2}^{net} .$$

# Concluding remarks I

## Summary:

- Climate policy is confronted with an equity-efficiency trade-off.
- A uniform price on carbon is efficient in the sense that it allows to reach national emission targets at minimal costs.
- Deviations to a sector-specific climate policy can be justified by distributive concerns.
- In the presence of non-linear income taxes, a second-best logic may imply that deviations from the market-based approach can be justified by efficiency considerations.

# Concluding remarks II

## Outside the model:

- A market-based approach to climate policy has advantages of simplicity and accountability. Those are not captured by the welfare analysis that is presented in this paper.
- As suggested by the welfare analysis in this paper, the distributive implications of such an approach may be perceived as unfair.
- Possibly this is an explanation for the lack of political support and the protests that are spurred by plans for more ambitious climate policies.
- Reaching emission targets in a politically feasible way may therefore require a sector-specific approach.