

# Pass-through as an Economic Tool

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# Wanted: IO theory for empirics

- Plea for IO theory to engage with structural IO
- IO theory boomed in 80's, declined since in US. Why?
  - You can prove anything!
    - E.g. Bulow et. al. (1985) and Fudenberg and Tirole (1984)
    - All depends on strategic complements v. substitutes...
    - But we don't know this
- So structural IO: figure out demand system (Bresnahan)
  - No need for theory, just computation (BLP)
  - But identification relies on strong assumptions
  - Assume the result sometimes?
- So theory comes back in: what, how to measure
- Implications of (functional form) assumptions
- Today: simple example
  - Demand shape restrictions important for theory

# Introduction

- So what should we measure?
- In competitive markets: elasticities
  - Tax revenues
  - Welfare (Chetty's sufficient statistics)
- But in IO elasticities = level not comparative statics
- *Pass-through* serves role of elasticities
  - 1 Many different theory results depend on it
  - 2 Basis for identification with weak assumptions
  - 3 Flexibility important, but rare: create demand systems

# Examples

- 1 Generalized Cournot-Stackelberg (GCS) models
  - Which side of  $1 + \text{sign of slope}$   $\implies$ 
    - Ranking of firm and industry markups/quantities and profits
- 2 Two-sided markets (Rochet and Tirole 2003)
  - Positive and normative properties: PT v. 1, sign of slope
- 3 Symmetric multiproduct models (Cournot or Bertrand)
  - Merger effects determined by PT
  - With horizontal demand
    - 1 Strategic complements v. substitutes: PT v. 1
    - 2 Short- and long-run idiosyncratic same side as industry PT
  - For example: many firm Berry, Levinsohn and Pakes (1995)
    - $\implies$  PT determines effect of entry, mergers on prices
      - Closely linked to log-curvature, so micro tests also
- 4 International macro: link to price frequency

# Overview

- 1 Review pass-through, new results on why matters
- 2 Illustrate with GCS models
- 3 Two generalizations
  - Two-sided markets
  - Multiple products, mergers
- 4 Taxonomy of functional forms
- 5 Apt demand
- 6 Conclusion and directions for research

# Monopoly pricing

$$m \equiv p - c = -\frac{D(p)}{D'(p)} \equiv \mu(p)$$

- Standard condition for sufficiency is log-concavity,  $\mu' < 0$ 
  - But *grossly* sufficient
  - $\rho \equiv \frac{dp_M}{dc} = \frac{1}{1-\mu'}$  so log-concave  $\iff$  “cost-absorbing”
- Weakest condition for same tractability gain:  
 $\mu' < 1 \iff MR'(Q) < 0 \iff \frac{1}{D}$  convex
  - Mark-up contraction (MUC)  
 $\iff$  Always charge at binding price control for all  $c$

# Useful properties of pass-through

Pass-through crucial parameter, two reasons:

- 1 Measures sharpness of monopoly problem

$$\rho = \frac{1}{-\frac{d^2\pi}{dm^2} \frac{m^2}{\pi}}$$

- Quantity parallel
- “Pass-through” of pre-existing units  $\rho_Q = \rho$

- 2 Determines division of surplus

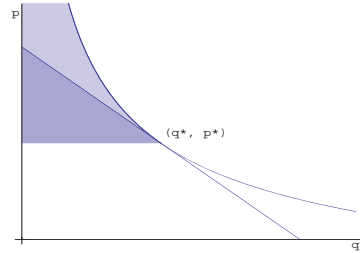
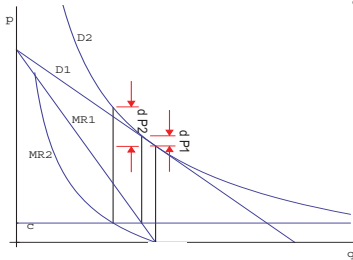
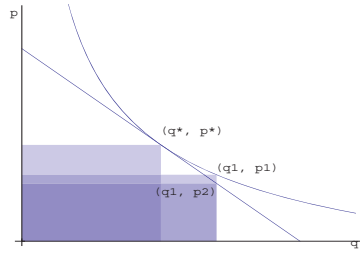
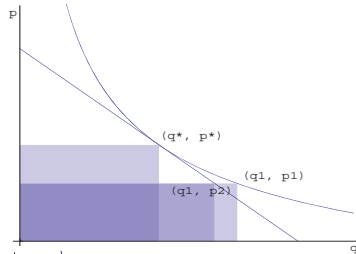
- Surplus  $V$  and profits  $\pi = \mu D$  (at optimal price)
- For all prices  $p < \bar{p}$  (choke price)

$$\frac{V(p)}{\mu(p)D(p)} = \bar{\rho}(p) \equiv \int_p^{\bar{p}} \lambda(q; p) \rho(q) dq$$

where  $\int_p^{\bar{p}} \lambda(q; p) dq = 1$

- Ratio of surpluses determined by average of pass-through
- Deadweight loss as well

# Graphical proof of pass-through properties





# Taxonomy of demand

- Three types of demand
  - 1  $\rho < 1 \iff \mu' < 0$ : cost absorption (Rochet-Tirole 2007)
  - 2  $\rho = 1 \iff \mu' = 0$ : constant mark-up
  - 3  $\rho > 1 \iff \mu' > 0$ : cost amplification
- Increasing vs. decreasing in cost

## Assumption

### *Demand globally one combination*

- Can be substantially weakened, but clean
- Obeyed by almost every demand (shown below)
- Which side does demand typically lie on?
  - CE amplifying, linear absorbing; both constant PT
  - Empirical evidence: little, roughly 70-30 absorbing
  - No evidence on slope

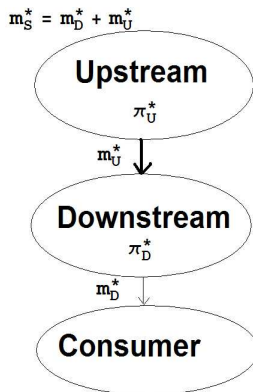
# Cournot (1838)-Spengler (1950) model

- Detailed, simple example to show how it works
  - Presented this last year, so go quick
  - But I have generalization
  - Of independent interest?
- Two goods:
  - Perfect complements (Cournot)
  - One input to other (Spengler)
- Total (linear) cost  $c_i$
- Baseline case integrated monopoly, optimal mark-up  $m_i^*$
- Two separated organizations

# Spengler-Stackelberg organization

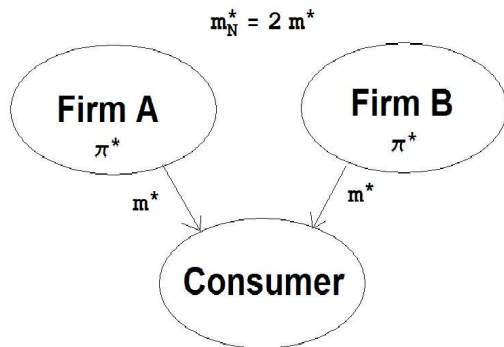
$$m_U^* = \frac{\mu(m_U^* + m_D^* + c_I)}{\rho(m_U^* + m_D^* + c_I)}$$

$$m_D^* = \mu(m_U^* + m_D^* + c_I)$$



# Cournot-Nash organization

$$m_A^* = \mu(m_A^* + m_B^* + c_I)$$
$$m_B^* = \mu(m_A^* + m_B^* + c_I)$$



# Graphical summary of results

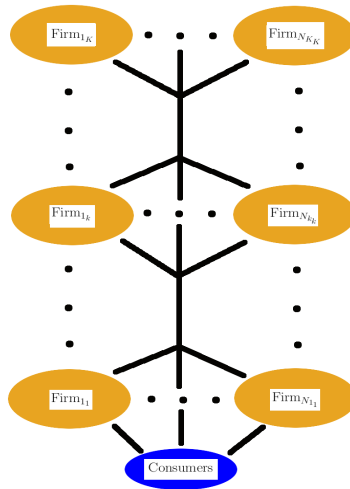
	$\rho < 1$	$\rho > 1$
	Cost absorption Decreasing pass-through	Cost amplification Decreasing pass-through
$\rho' \wedge 0$	$m_U^*$ $\vee$ $m_I^* < m_N^* < m_S^*$ $\vee$ $m^*$ $\vee$ $m_D^*$	$m^*$ $\vee$ $m_D^*$ $\vee$ $m_U^*$ $\vee$ $m_I^* < m_S^* < m_N^*$
	$\pi_U^*$ $\vee$ $\pi^*$ $\vee$ $\pi_D^*$	$\pi_D^*$ $\vee$ $\pi_U^*$ $\vee$ $\pi^*$
	Cost absorption Increasing pass-through	Cost amplification Increasing pass-through
$\rho' \vee 0$	$m_I^* < m_N^* < m_S^*$ $\vee$ $m_U^*$ $\vee$ $m^*$ $\vee$ $m_D^*$	$m^*$ $\vee$ $m_D^*$ $\vee$ $m_I^* < m_S^* < m_N^*$ $\vee$ $m_U^*$
	$\pi_U^*$ $\vee$ $\pi^*$ $\vee$ $\pi_D^*$	$\pi_D^*$ $\vee$ $\pi_U^*$ $\vee$ $\pi^*$

**Table:** A taxonomy of the Cournot-Spengler double marginalization

# Explaining the results

- $\pi_U^* > \pi^*$
- $\rho$  v. 1 crucial
  - Determines strategic complements v. substitutes
  - $m^*$  v.  $m_I^*$ : magnify or absorb 2nd mark-up
  - $m_U^*$  v.  $m_D^*$  ( $\pi_U^*$  v.  $\pi_D^*$ ): what lowers  $m_D^*$ ?
  - Everything else except  $m_U^*$  v.  $m_I^*$  determined by same
- $m_U^*$  v.  $m_I^*$  more subtle
  - How much of  $m_D$  to pass-through vs. strategic effect
  - Marginal vs. average
    - Pass-through increasing or decreasing?

# Generalization to GCS models



# Quantity competition: Sonnenschein (1968)

Double marginalization = dual of quantity competition

⇒ Switching quantity for mark-up, all results here hold with  $\rho_Q$

- But how to identify  $\rho_Q, \rho'_Q$ ?
- Cost shocks work just as well
  - Firm specific cost shock:  $\frac{dq}{dc} = -\frac{m^*}{q^*} \frac{dq}{dc}$
  - Works for general GCS model
  - Intuition: link between cost-price and quantity pass-through
- Thus identification proceeds in *exactly* same way



## Two-sided markets

- More at comp. policy seminar (June 12) on RT2006
  - ⇒ Source of heterogeneity really important
- Special case of RT2003: only usage values (heterogeneity)
  - Visa and cross-subsidies
  - Only cross-effect
    - ⇒ Pass-through of cross-subsidies crucial
  - Externality=average surplus, only marginal internalized
    - Also determined by pass-through!
    - ⇒ Much turns on pass-through, slope

# Mergers

## Static unilateral effects of mergers from Bertrand competition

- How much are efficiencies passed-through?
- Anti-competitive effect is opportunity cost from diversion (Froeb et. al. 2005, Farrell and Shapiro 2008)  
 ⇒ Diversion-efficiencies=sign, pass-through=magnitude
- Avoids pitfalls of functional form, but ignores...
  - Interactions between anti-competitive effects
  - Effects on (and through) other firms' pricing
- To solve, new “constant pass-through demand system”
  - $D^i(\mathbf{p}) = \lambda \left( [\rho_i - 1] \left[ p_i + \sum_{j \neq i} \beta_{ji} p_j - \tilde{p}_i \right] \right)^{\frac{\rho_i}{1-\rho_i}}$
  - Allows full variation in pass-through
  - Also useful: linearity, second-order conditions, mergers, etc.
  - Works for differentiated Cournot as well
  - But no Slutsky symmetry

# Symmetric horizontal demand systems

- General theories: Bertrand/Cournot with arbitrary demand
  - Little first-order empirical content (from cost shocks)
    - E.g. Bulow et. al. (1985), Fudenberg and Tirole (1984)
    - How to figure out strategic substitutes v. complements?
  - Only stability-based inequalities, positive idiosyncratic PT
- With a bit more structure gives a lot of identification
  - Working to generalize...
- Two assumptions:
  - 1 Symmetry across firms
  - 2 Horizontal demand system
    - $D_i(p_i, \mathbf{p}) = \tilde{D}(p_i - g[\mathbf{p}_{-i}])$
    - Increasing price of substitute increases willingness to pay
    - Linear, CoPaDS special cases

# Results with symmetric horizontal demand

Under these assumptions

- 1 Three notions of PT all on same side of 1:
  - 1 *Short-run own* (Sop)
  - 2 *Long-run own* (Lop)
  - 3 *Industry* (in symmetric model)
- 2 Pass-through + Bertrand v. Cournot  $\implies$  strategic effect
  - Thus “conventional wisdom” reversed when  $\rho > 1$
  - Identifies lots (Bulow et. al. and Fudenberg and Tirole)
- 3 Effects of entry, merger on other prices

		$\rho < 1$	
		Substitutes	Complements
	Bertrand	Strategic complements	Strategic substitutes
	Cournot	Strategic substitutes	Strategic complements

		$\rho > 1$	
		Substitutes	Complements
	Bertrand	Strategic substitutes	Strategic complements
	Cournot	Strategic complements	Strategic substitutes

# Effects of market conditions on pass-through

- Also how primitives affect various pass-through rates
- *Assuming constant marginal cost:*
  - ①  $Sop \uparrow \implies Lop, \text{ industry } \uparrow, \text{ more strategic substitutes}$
  - ②  $N \uparrow Lop, \text{ industry } \downarrow, \text{ less interaction}$
  - ③  $\text{Less differentiation} \implies \text{industry} \rightarrow 1, Lop \uparrow$ 
    - Counterintuitive? See below
    - Can't pass-through, but can't afford not to
- Strategic effects opposite when complements
- When marginal cost non-constant
  - Increasing marginal cost just like low pass-through
  - Increasing competition makes cost more important
  - Competitive, near constant MC  $\implies$  compare elasticities

# Discrete choice models

Most empirical work uses discrete choice models

- These models are hard to analyze for pricing
- But using recent formula of Gabaix et. al. (2009) by EVT....
- Non-parametric symmetric many firm BLP is horizontal
- We think more complicated may as well
  - Intuitive link
- Robust preservation of log-concavity under transformations
  - ⇒ Demand same log-curvature as idiosyncratic errors
    - Assumptions about errors ⇒ assumption on demand
    - May give test for PT based on discrete choice
- Effect of competition on prices driven by log-curvature
  - Strategic complementarity vs. substitution
- So allowing flexibility in pass-through, slope important...

# Common demand functions

	$\rho < 1$	$\rho > 1$	Price-dependent
$\rho' \wedge 0$			AIDS
$\rho' \vee 0$	Normal (Gaussian) Logistic Type I Extreme Value (Gumbel) Double Exponential Type III Extreme Value (Reverse Weibull) Weibull with shape $\alpha > 1$ Gamma with shape $\alpha > 1$		Type II Extreme Value (Fréchet) with shape $\alpha > 1$
Price-dependent			
Does not globally satisfy MUC		Type II Extreme Value (Fréchet) with shape $\alpha < 1$ Weibull with shape $\alpha < 1$ Gamma with shape $\alpha < 1$	

# Apt demand (with Fabinger)

How can we get flexibility (and tractability)?

- Generalize Bulow-Pfleiderer constant PT demand

$$D(p) = \lambda \left( |\bar{p} - 1| \sqrt{|p - \tilde{p}|} - 2\bar{p}\alpha \right)^{\frac{2\bar{p}}{1-\bar{p}}}$$

- Apt demand (modulo technicalities)
- Also inverse demand formulation



# Properties of Apt demand

Many nice properties

- 1 All nice standard demand assumptions
- 2 Flexible on level, elasticity, PT and slope of PT
- 3 Quadratic solutions to monopoly pricing
  - And simple explicit solution to very wide range
- 4 Generalizes all known tractable demand (Bulow-Pfleiderer)
  - Linear
  - Constant elasticity
  - Negative exponential
- 5 Easily estimated
- 6 Simple closed form surplus, estimates from formula
- 7 Software we made makes easy to use (June 17 seminar)

## Where now?

### Important direct extensions

- 1 Non-symmetric multi-product models
- 2 More general connection to discrete choice/empirical IO
  - Vertical differentiation (Bennot had thought)
- 3 Demand systems: discrete choice

### Others' applications

- 1 Price frequency + pass-through (Gopinath-Itzhak)
- 2 Third-degree price discrimination (Aguirre, Cowan, Vickers)
- 3 Price controls on consumer welfare (Bulow-Klemperer)

### Where future might go

- Identifying assumptions
  - Statistical relaxations
  - Economic foundations
- Auction theory? Public finance?