

Table 1(a). Simulation Means and Standard Deviations of $2SQRI(\theta, q = 1) : N(0,1)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	-0.75	-0.35	-0.01	0.31	0.77
		Std	2.18	1.15	0.83	0.67	0.58
	$\tilde{\beta}_1$	Mean	0.01	0.00	0.00	0.00	0.00
		Std	0.35	0.23	0.21	0.23	0.35
	$\tilde{\gamma}$	Mean	-0.01	0.00	0.00	0.01	0.00
		Std	0.51	0.34	0.31	0.33	0.49
$T = 300$	$\tilde{\beta}_0$	Mean	-0.84	-0.34	-0.01	0.33	0.81
		Std	0.83	0.43	0.33	0.26	0.22
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.14	0.09	0.09	0.09	0.13
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.01
		Std	0.19	0.12	0.12	0.13	0.19

Table 1(b). Simulation Means and Standard Deviations of $2SQRI(\theta, q = q^*) : N(0,1)$.

		θ (q^*)	0.05 (0.0013)	0.25 (-0.0003)	0.50 (0.0002)	0.75 (0.0003)	0.95 (0.0027)
$T = 50$	$\tilde{\beta}_0$	Mean	0.59	0.23	-0.01	-0.26	-0.62
		Std	1.19	0.89	0.71	0.54	0.36
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.19	0.19	0.18	0.18	0.19
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.27	0.26	0.26	0.26	0.27
$T = 300$	$\tilde{\beta}_0$	Mean	0.72	0.29	-0.01	-0.31	-0.74
		Std	0.44	0.34	0.27	0.21	0.14
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.07	0.07	0.07	0.07	0.07
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.10	0.10	0.10	0.10	0.10

Table 1(c). Simulation Means and Standard Deviations of $2SQRI(\theta, q = \hat{q}) : N(0,1)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	0.22	0.15	-0.01	-0.20	-0.26
		Std	1.49	0.91	0.72	0.54	0.40
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.22	0.19	0.18	0.19	0.22
	$\tilde{\gamma}$	Mean	0.01	0.01	0.00	0.01	0.01
		Std	0.33	0.26	0.26	0.27	0.32
	\hat{q}	Mean	0.19	-0.01	-0.05	0.07	0.31
		Std	0.33	0.23	0.20	0.20	0.20
$T = 300$	$\tilde{\beta}_0$	Mean	0.62	0.25	-0.01	-0.27	-0.62
		Std	0.46	0.34	0.27	0.21	0.16
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.07	0.07	0.07	0.07	0.07
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.10	0.10	0.10	0.10	0.10
	\hat{q}	Mean	0.08	0.00	-0.05	0.00	0.10
		Std	0.09	0.11	0.12	0.11	0.09

Table 2(a). Simulation Means and Standard Deviations of $2SQRI(\theta, q = 1) : t(3)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	-1.07	-0.34	0.01	0.42	1.36
		Std	7.32	2.04	1.42	1.06	1.05
	$\tilde{\beta}_1$	Mean	0.04	0.02	0.01	-0.01	-0.01
		Std	0.88	0.33	0.28	0.34	0.85
	$\tilde{\gamma}$	Mean	-0.06	-0.02	-0.01	-0.01	-0.1
		Std	1.48	0.59	0.51	0.54	1.43
$T = 300$	$\tilde{\beta}_0$	Mean	-1.18	-0.40	-0.02	0.37	1.20
		Std	2.17	0.59	0.40	0.33	0.33
	$\tilde{\beta}_1$	Mean	0.02	0.00	0.00	0.00	0.00
		Std	0.29	0.11	0.10	0.12	0.30
	$\tilde{\gamma}$	Mean	0.00	0.00	0.01	0.01	0.01
		Std	0.43	0.17	0.14	0.17	0.42

Table 2(b). Simulation Means and Standard Deviations of $2SQRI(\theta, q = q^*) : t(3)$.

		θ (q^*)	0.05 (-0.079)	0.25 (0.537)	0.50 (0.835)	0.75 (0.538)	0.95 (-0.078)
$T = 50$	$\tilde{\beta}_0$	Mean	0.90	0.01	0.02	0.10	-0.74
		Std	2.98	1.89	1.42	1.00	0.43
	$\tilde{\beta}_1$	Mean	0.02	0.02	0.01	0.01	0.02
		Std	0.35	0.32	0.28	0.31	0.34
	$\tilde{\gamma}$	Mean	-0.03	-0.02	-0.01	-0.02	-0.03
		Std	0.58	0.55	0.51	0.50	0.53
$T = 300$	$\tilde{\beta}_0$	Mean	0.87	-0.06	-0.02	0.02	-0.92
		Std	0.94	0.56	0.40	0.32	0.16
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.12	0.11	0.10	0.11	0.12
	$\tilde{\gamma}$	Mean	0.01	0.01	0.01	0.01	0.01
		Std	0.18	0.16	0.14	0.16	0.18

Table 2(c). Simulation Means and Standard Deviations of $2SQRI(\theta, q = \hat{q}) : t(3)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	-0.19	0.10	0.07	-0.01	-0.22
		Std	13.6	2.02	1.66	1.04	0.86
	$\tilde{\beta}_1$	Mean	0.03	0.01	0.01	0.01	0.01
		Std	0.56	0.30	0.31	0.31	0.52
	$\tilde{\gamma}$	Mean	0.07	-0.01	-0.02	-0.02	-0.01
		Std	2.74	0.58	0.59	0.52	1.19
	\hat{q}	Mean	0.19	0.30	0.32	0.32	0.29
		Std	0.54	0.30	0.27	0.28	0.37
$T = 300$	$\tilde{\beta}_0$	Mean	0.80	0.01	-0.01	-0.04	-0.87
		Std	1.02	0.57	0.40	0.33	0.29
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.12	0.11	0.10	0.11	0.13
	$\tilde{\gamma}$	Mean	0.01	0.01	0.00	0.00	0.01
		Std	0.19	0.16	0.15	0.16	0.19
	\hat{q}	Mean	0.01	0.45	0.57	0.44	0.04
		Std	0.16	0.18	0.16	0.18	0.16

Table 3(a). Simulation Means and Standard Deviations of $2SQRI(\theta, q = 1) : LN(0,1)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	-0.50	-0.35	-0.10	0.37	2.00
		Std	1.43	1.26	1.56	2.06	3.00
	$\tilde{\beta}_1$	Mean	0.02	0.02	0.02	0.01	0.03
		Std	0.21	0.21	0.30	0.48	1.73
	$\tilde{\gamma}$	Mean	-0.05	-0.05	-0.05	-0.05	-0.14
		Std	0.35	0.33	0.47	0.88	2.64
$T = 300$	$\tilde{\beta}_0$	Mean	-0.74	-0.57	-0.33	0.15	1.85
		Std	0.49	0.50	0.56	0.66	1.08
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.01	0.02
		Std	0.08	0.09	0.11	0.19	0.65
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.01	0.02
		Std	0.11	0.13	0.16	0.27	0.91

Table 3(b). Simulation Means and Standard Deviations of $2SQRI(\theta, q = q^*) : LN(0,1)$.

		θ (q^*)	0.05 (1.0388)	0.25 (1.051)	0.50 (0.972)	0.75 (0.167)	0.95 (-0.146)
$T = 50$	$\tilde{\beta}_0$	Mean	-0.56	-0.41	-0.08	0.18	-1.25
		Std	1.41	1.25	1.56	1.57	0.91
	$\tilde{\beta}_1$	Mean	0.02	0.02	0.02	0.02	0.03
		Std	0.21	0.21	0.30	0.40	0.45
	$\tilde{\gamma}$	Mean	-0.05	-0.04	-0.05	-0.06	-0.07
		Std	0.35	0.33	0.47	0.65	0.71
$T = 300$	$\tilde{\beta}_0$	Mean	-0.79	-0.62	-0.31	-0.08	-1.42
		Std	0.49	0.50	0.56	0.54	0.32
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.08	0.09	0.11	0.16	0.18
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.01
		Std	0.11	0.13	0.16	0.22	0.24

Table 3(c). Simulation Means and Standard Deviations of $2SQRI(\theta, q = \hat{q}) : LN(0,1)$.

		θ	0.05	0.25	0.50	0.75	0.95
$T = 50$	$\tilde{\beta}_0$	Mean	-0.39	0.04	0.18	0.21	-1.01
		Std	1.55	1.58	2.20	2.38	1.82
	$\tilde{\beta}_1$	Mean	0.02	0.02	0.02	0.02	0.02
		Std	0.22	0.25	0.34	0.40	0.75
	$\tilde{\gamma}$	Mean	-0.06	-0.05	-0.06	-0.07	-0.11
		Std	0.37	0.41	0.66	1.01	2.06
	\hat{q}	Mean	0.92	0.65	0.55	0.28	0.02
		Std	0.11	0.13	0.25	0.40	0.37
$T = 300$	$\tilde{\beta}_0$	Mean	-0.68	-0.40	-0.23	-0.03	-1.37
		Std	0.50	0.52	0.56	0.55	0.37
	$\tilde{\beta}_1$	Mean	0.00	0.00	0.00	0.00	0.00
		Std	0.09	0.09	0.11	0.16	0.18
	$\tilde{\gamma}$	Mean	0.00	0.00	0.00	0.00	0.01
		Std	0.12	0.13	0.16	0.23	0.25
	\hat{q}	Mean	0.96	0.85	0.85	0.38	-0.17
		Std	0.04	0.04	0.06	0.31	0.08

Table 4(a). Simulated Standard Deviations of 2SQR1 (θ, \hat{q}) and Cramer-Rao Bounds with $T = 50$

Estimator	First Stage	Second Stage		N(0,1)	$t(3)$	LN(0,1)
CR bounds			$\hat{\beta}_1$	0.19	0.20	0.04
			$\hat{\gamma}$	0.26	0.28	0.06
2SLS	LS	LS	$\hat{\beta}_1$	0.21	0.41	0.42
			$\hat{\gamma}$	0.30	0.78	0.70
2SQR(θ, \hat{q})	LS	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.22	0.56	0.22
			$\hat{\gamma}$	0.33	2.74	0.37
2SQR(θ, \hat{q})	LS	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.19	0.30	0.25
			$\hat{\gamma}$	0.26	0.58	0.41
2SQR(θ, \hat{q})	LS	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.19	0.31	0.34
			$\hat{\gamma}$	0.26	0.59	0.66
2SQR(θ, \hat{q})	LS	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.19	0.31	0.40
			$\hat{\gamma}$	0.27	0.52	1.01
2SQR(θ, \hat{q})	LS	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.22	0.52	0.75
			$\hat{\gamma}$	0.32	1.19	2.06

Table 4(b). Simulated Standard Deviations of 2SQR2 (θ, q) with $T = 50$

Estimator	First Stage	Second Stage		N(0,1)	$t(3)$	LN(0,1)
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.36	0.82	0.15
			$\hat{\gamma}$	0.52	1.22	0.22
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.24	0.31	0.17
			$\hat{\gamma}$	0.37	0.44	0.25
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.23	0.24	0.23
			$\hat{\gamma}$	0.36	0.39	0.35
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.24	0.31	0.42
			$\hat{\gamma}$	0.37	0.48	0.63
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.35	0.79	1.63
			$\hat{\gamma}$	0.51	1.14	2.33
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.24	0.51	0.15
			$\hat{\gamma}$	0.40	0.85	0.23
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.21	0.26	0.18
			$\hat{\gamma}$	0.36	0.39	0.27
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.21	0.24	0.23
			$\hat{\gamma}$	0.34	0.44	0.35
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.22	0.26	0.29
			$\hat{\gamma}$	0.36	0.40	0.46
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.23	0.36	0.46
			$\hat{\gamma}$	0.36	0.53	0.65

Table 5(a). Simulated Standard Deviations of 2SQR1 (θ, \hat{q}) and Cramer-Rao Bounds with $T = 300$

Estimator	First Stage	Second Stage		N(0,1)	$t(3)$	LN(0,1)
CR bounds			$\hat{\beta}_1$	0.07	0.08	0.02
			$\hat{\gamma}$	0.10	0.12	0.02
2SLS	LS	LS	$\hat{\beta}_1$	0.07	0.12	0.16
			$\hat{\gamma}$	0.10	0.18	0.22
2SQR (θ, \hat{q})	LS	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.07	0.12	0.09
			$\hat{\gamma}$	0.10	0.19	0.12
2SQR (θ, \hat{q})	LS	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.07	0.11	0.09
			$\hat{\gamma}$	0.10	0.16	0.13
2SQR (θ, \hat{q})	LS	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.07	0.10	0.11
			$\hat{\gamma}$	0.10	0.15	0.16
2SQR (θ, \hat{q})	LS	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.07	0.11	0.16
			$\hat{\gamma}$	0.10	0.16	0.23
2SQR (θ, \hat{q})	LS	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.07	0.13	0.18
			$\hat{\gamma}$	0.10	0.19	0.25

Table 5(b). Simulated Standard Deviations of 2SQR2 (θ, q) with $T = 300$

Estimator	First Stage	Second Stage		N(0,1)	$t(3)$	LN(0,1)
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.14	0.28	0.05
			$\hat{\gamma}$	0.20	0.42	0.07
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.09	0.11	0.06
			$\hat{\gamma}$	0.13	0.16	0.08
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.09	0.09	0.09
			$\hat{\gamma}$	0.12	0.13	0.12
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.09	0.11	0.17
			$\hat{\gamma}$	0.13	0.16	0.24
Trim(φ)-2SQR($\theta, 1$)	Trim(0.25)	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.13	0.30	0.62
			$\hat{\gamma}$	0.19	0.41	0.89
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.05$)	$\hat{\beta}_1$	0.08	0.10	0.05
			$\hat{\gamma}$	0.11	0.14	0.07
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.25$)	$\hat{\beta}_1$	0.08	0.09	0.06
			$\hat{\gamma}$	0.11	0.13	0.08
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.50$)	$\hat{\beta}_1$	0.08	0.09	0.09
			$\hat{\gamma}$	0.11	0.13	0.12
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.75$)	$\hat{\beta}_1$	0.08	0.09	0.12
			$\hat{\gamma}$	0.11	0.13	0.17
Trim(φ)-2SQR(θ, \hat{q})	Trim(0.25)	Quantile($\theta=0.95$)	$\hat{\beta}_1$	0.08	0.10	0.10
			$\hat{\gamma}$	0.11	0.14	0.14