# Buyer power from joint listing decision

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#### Abstract

We show that collective bargaining can enhance retailers' buying power vis-àvis their suppliers. We consider a model of vertically related markets, in which an upstream leader faces a competitive fringe of less efficient suppliers and negotiates secretly with several firms that compete in a downstream market. We allow downstream firms to join forces in negotiating with suppliers, by creating a buyer group which selects suppliers on behalf of its members: each group member can then veto the upstream leader's offer, in which case all group members turn to the fringe suppliers. Transforming individual listing decisions into a joint listing decision makes delisting less harmful for a group member; this, in turn enhances the group members' bargaining position at the expense of the upstream leader. We also show that this additional buyer power can have an ambiguous impact on the upstream leader's incentives to invest.

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### 1 Introduction

During the last decades, retailers have increasingly sought to join forces so as to enhance their buyer power vis-à-vis suppliers. In Europe, the grocery industry has seen the

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emergence of several chains of independent supermarkets such as Leclerc and Système U in France, who in 1999 joined their forces further in a buying alliance called Lucie;<sup>1</sup> similarly, in Finland the two leading voluntary retail chains, Kesko and Tuko, attempted to merge in 1996.<sup>2</sup> In the US, independent retail grocers, including the Independent Grocers Association (IGA) have long used buyer groups to negotiate with suppliers.<sup>3</sup> Other retailing industries have undergone some consolidation as well. In France, for instance, the pharmaceutical retailing industry has seen the emergence of some buyer groups (Astera, Giphar, and Giropharm).<sup>4</sup>

These retailers thus rely on collective bargaining in order to gain buying power. Two commonly recognized benefits of such collective bargaining are the associated economies of scale and the ability to make a joint listing decision (or more precisely, a joint delisting decision, as we will see below). Economies of scale arise for example from common operational costs.<sup>5</sup> The ability to make a joint (de-)listing decision arises when a group of individual retailers can commit to a decision that binds all of its members. While economies of scale clearly bring benefits to buyer groups, whether joint listing decisions do so is less clear.

The objective of this paper is to explore when and how joint delisting decision can affect bargaining position of the buyer group, and whether larger buyer group benefits more of such joint delisting decisions. We consider a model of vertically related markets à la Rey and Tirole (2007), in which manufacturers compete by simultaneous making secret offers. Upstream, a market leader faces a competitive fringe of less efficient suppliers; downstream, firms compete and use the suppliers' input to produce a homogeneous good. We allow a number of downstream firms to join forces in negotiating with the upstream leader: they create a buyer group, which selects suppliers on behalf of its members. More precisely, we focus on a listing rule where each group member can veto the upstream leader, in which case all group members turn to the fringe suppliers and

<sup>&</sup>lt;sup>1</sup>This buying alliance was dissolved in 2006, when Système U joined a European buying alliance (European Market Distribution) with another French retailing competitor, Casino. Leclerc, Système U and Casino accounted respectively for 17%, 9% and 10% of sales in French grocery and daily goods retailing in 2009 (TNS Worldpanel).

 $<sup>^{2}</sup>$ The concentration was canceled by the European Commission (Case IV/M.784).

<sup>&</sup>lt;sup>3</sup>IGA is the world's largest voluntary supermarket chain with more than 5,000 member stores.

 $<sup>^4\</sup>mathrm{Astera,}$  Giphar, and Giropharm represent around 20% of the pharmaceutical retailing industry in France.

<sup>&</sup>lt;sup>5</sup>Retailers can share other fixed costs. For example, they may have economies of scale in finding or setting-up an alternative source of supply (see Katz, 1987 and Sheffman and Spiller, 1992).

also show that this rule enhances the bargaining position of the buyer group. Intuitively, transforming individual delisting decision into a joint boycott makes such a decision less harmful for a group member, since the other group members will also have to deal with the alternative, less efficient supplier. This, in turn, enhances the group members' bargaining position, by raising the value of their outside options. In our model (where secret contracting implies that the marginal input price always reflects the upstream marginal cost), this better bargaining position does not lead to lower prices for consumers. This is in line with the concern voiced by antitrust authorities; for example, the European Commission states in its Guidelines: "cost savings or other efficiencies that only benefit the parties to the joint purchasing arrangement will not suffice. Cost savings need to be passed on to consumers".<sup>6</sup>

The literature has used various way to generate size-related discounts. Katz (1987) models buyer power as a retailer's ability to integrate backwards by paying a fixed cost. Getting larger reduces the average cost of this alternative option and allows in this way the retailer to obtain a better price from the supplier.<sup>7</sup> Size may not only increase the value of a retailer's alternatives but also reduce the suppliers' alternatives. If the supplier's cost is convex, then dealing with a larger retailer reduces the (average) avoidable cost that is at stake, which weakens the seller's bargaining position; the retailer thus benefits from its larger size (Chipty and Snyder (1999));<sup>8</sup> similarly, when the negotiation breaks down with a large buyer, re-allocating production to the other buyers may be less valuable (Inderst and Wey (2007)). Inderst and Shaffer (2007) and Dana (2009) relate instead buyer power to the possibility, for a large buyer, to reduce the number of suppliers which it deals with.

These approaches focus on "pure" buyer power, in the sense that group members only interact on the buying side.<sup>9</sup> Dobson and Waterson (1997) and von Ungern-Sternberg (1996) consider instead "full mergers", in which the downstream firms not only join forces as buyers, but also eliminate competition between them as sellers. By contrast,

 $<sup>^{6}</sup>$ Guidelines on the applicability of Article 101 of the Treaty on the Functionning of the European Union to horizontal co-operation agreements (2011/C 11/01), paragraph 219.

<sup>&</sup>lt;sup>7</sup>See Inderst and Valletti (2011) and Inderst and Wey (2011) for recent contributions that build on this insight.

 $<sup>^{8}</sup>$ See Smith and Thanassoulis (2011) and Bedre and Caprice (2011) for recent contributions along this line.

<sup>&</sup>lt;sup>9</sup>That is, while group members may be competing in their respective downstream markets, they are not competing against each other in the same markets.

we focus in this paper on the bargaining power that buyer groups confer to firms that are and remain competitors in the same downstream market.

We also study the implications of our analysis for upstream investment incentives. As in Inderst and Wey (2011), downstream competition tends to induce suppliers to overinvest in productivity, since this reduces downstream firms' outside options and thus allows the suppliers to obtain a bigger share of the industry profit. As in their paper, we also find that increasing the size of the buyer group can exacerbate this over-investment incentive; however, when the buyer group already involves a large proportion of the downstream firms, increasing its size further tends to eliminate the above mechanism (indeed, if all downstream firms join the buyer group, their outside option is no longer affected by the supplier's own productivity), which reduces investment incentives. This is in line with the concern, frequently expressed in policy circles, that suppliers respond to the exercise of buyer power "by under-investing in innovation and production" (FTC 2001, p.57).

The rest of the paper is organized as follows. We first present our framework (section 2), before showing how joint listing decisions benefit group members when they also compete against each other in the same downstream markets (section 3). Results are discussed and extended in section 4. We then build on this analysis to study the impact of buyer groups on suppliers investment (section 5). Section 6 concludes.

## 2 A simple framework

We consider two vertically related markets. In the upstream market a leader, U, faces a constant marginal cost of production c, whereas a competitive fringe,  $\hat{U}$ , supplies at cost  $\hat{c} > c$ . In the downstream market n competitors,  $D_1, ..., D_n$ , transform the intermediate product into a homogenous final good, on a one-to-one basis and at no additional cost. We assume that the inverse demand for the final good, denoted by p = P(Q), satisfies the following regularity conditions:

Assumption 1: P(0) > c and, for any  $Q \ge 0$ :

$$P'(Q) < 0 \text{ and } P'(Q) + P''(Q) Q < 0.$$

This standard assumption first states that the industry is viable and demand is strictly decreasing; the last part implies that downstream equilibria are well-behaved. In particular, it implies that the profit function

$$\pi\left(q_{i};Q_{-i},c\right)\equiv\left[P\left(Q_{-i}+q_{i}\right)-c\right]q_{i}$$

is strictly concave, and that a symmetric Cournot oligopoly, in which all firms face the same cost c, has a unique, symmetric and stable equilibrium,<sup>10</sup> in which each firm sells  $q^{C}(c)$ , solution to  $q^{C} = R^{C}((n-1)q^{C}; c)$ , where

$$R^{C}(Q_{-i};c) \equiv \arg\max_{q_{i} \ge 0} \pi\left(q_{i};Q_{-i},c\right)$$

denotes the standard Cournot best response to rivals' aggregate quantity  $Q_{-i}$ . Dropping the argument c unless explicitly needed, we will denote by  $Q^C \equiv nq^C$ ,  $p^C \equiv P(Q^C)$ , and  $\Pi^C \equiv (p^C - c) Q^C$  the associated aggregate output, price and profit; the per-firm profit is then:

$$\pi^C \equiv \left( p^C - c \right) q^C.$$

We will assume that wholesale contracts are secret and consider the following competition game:

- Step 1: (a) U secretly offers each  $D_i$  a tariff  $T_i(.)$ ; (b) Each  $D_i$  secretly accepts or rejects U's offer.
- Step 2: Each  $D_i$  secretly orders a quantity  $\hat{q}_i$  from the fringe and, if it has accepted  $T_i(.)$ , a quantity  $q_i$  from U; the downstream firms then transform the intermediate product into final good, observe the total output Q and sell their own output at price P(Q).

As is well-known,<sup>11</sup> secret contracting creates a risk of opportunism: since  $D_i$ 's rivals do not observe neither U's offer nor  $D_i$ 's acceptance decision, in their bilateral negotiation U and  $D_i$  have an incentive to free-ride on downstream rivals' margins; but this, in turn, prevents U from fully exerting its market power. The extent to which this is the case

<sup>&</sup>lt;sup>10</sup>See Lemma 2 (with s = n) for a formal proof.

<sup>&</sup>lt;sup>11</sup>See the seminal paper from Hart and Tirole (1990), as well as O'Brien and Shaffer (1992) and McAfee and Schwartz (1994). Rey and Tirole (2007) provides an overview of this literature.

depends on how downstream firms interpret unexpected offers; for the sake of exposition, we will focus here on *passive conjectures* and thus assume that downstream firms stick to their equilibrium beliefs.<sup>12</sup> A downstream firm  $D_i$ , anticipating an aggregate equilibrium output  $Q_{-i}$  from its rivals, is then willing to pay  $P(Q_{-i} + q_i) q_i - \max_q \pi(q; Q_{-i}, \hat{c})$  for any quantity  $q_i$ , which leads the more efficient supplier, U, to supply  $q_i = R^C (Q_{-i}; c)$ .<sup>13</sup> It follows that the resulting equilibrium yields the Cournot outcome:

**Proposition 1** Under passive conjectures, the above competition game has a unique subgame perfect equilibrium outcome, in which:

(i) each  $D_i$  sells the competitive quantity  $q^C$ , which it buys from U;

(ii) each  $D_i$  earns the profit it could obtain by turning instead to the competitive fringe:

$$\hat{\pi} \equiv \max_{q \ge 0} \pi \left( q; (n-1) q^C, \hat{c} \right)$$

**Proof.** See Hart and Tirole (1990). ■

### 3 Buyer group

We now suppose that, in order to join forces in their negotiation with  $U, s \leq n$  downstream firms form a buyer group G, which will select suppliers on behalf of its members. To reflect this, we adapt the first step of the competition game as follows:

- Step 1a: as before; in particular, each group member only observes the offer it receives, not the offers made to the other members.
- Step 1b: Each group member recommends whether to accept or reject U's offers to the group G; these offers are all accepted if members unanimously recommend

$$P\left(Q_{-i} + R^{C}(Q_{-i};c)\right) R^{C}(Q_{-i};c) - \max_{q} \pi\left(q;Q_{-i},\hat{c}\right)$$
  
=  $cR^{C}(Q_{-i};c) + \max_{q} \pi\left(q;Q_{-i},c\right) - \max_{q} \pi\left(q;Q_{-i},\hat{c}\right)$   
 $\geq cR^{C}(Q_{-i};c).$ 

 $<sup>^{12}</sup>$ When downstream firms compete in quantities in a Cournot fashion, passive beliefs correspond to the wary beliefs introduced by McAfee and Schwartz (1994).

 $<sup>^{13}</sup>U$  finds indeed it profitable to supply  $D_i$ , since it can charge

doing so, and all rejected otherwise. The other downstream firms decide individually whether to accept the offer they received. Acceptance decisions are again private information: members of the buyer group know whether U's offers have been accepted by the group, but do not observe non-members' decisions, and these firms only observe their own decisions.

That is, we assume that contract offers remain secret, even within the group (we discuss in the next section the additional effects that arise when contract offers are observed within the group). However, each group member can now veto U's offers to the group, in which case all group members must turn to the less efficient fringe suppliers. Members' outside options are thus the outcome of the following oligopoly game, in which s group members face a cost  $\hat{c}$  and compete in quantities among themselves, anticipating that outsiders put on the market a given total quantity  $Q_o$ :

**Lemma 2** Suppose that the s members of the buyer group, facing the same cost  $\hat{c}$  and anticipating an output level  $Q_o$  from firms outside the group, compete in quantities among themselves; then:

(i) This competition yields a unique, stable equilibrium, in which each group member sells  $q^s = q^s (Q_o, \hat{c})$ , satisfying

$$q^{s} \equiv R^{C} \left( Q_{o} + (s-1) q^{s}; \hat{c} \right).$$

$$\tag{1}$$

(ii) Furthermore, letting  $\pi^s(Q_o, \hat{c}) \equiv (P(Q_o + sq^s(Q_o, \hat{c})) - \hat{c}) q^s(Q_o, \hat{c})$  denote the associated profit for each member, we have:

- $q^s(Q_o, \hat{c}) > 0$  (and thus  $\pi^s(Q_o, \hat{c}) > 0$ ) if and only if  $P(Q_o) > \hat{c}$ ;
- whenever  $P(Q_o) > \hat{c}$ ,

$$\frac{\partial q^s}{\partial Q_o}, \frac{\partial q^s}{\partial \hat{c}} < 0 \ and \ \frac{\partial \pi^s}{\partial Q_o}, \frac{\partial \pi^s}{\partial \hat{c}} < 0.$$

#### **Proof.** See Appendix A.

Obviously, there always exists trivial equilibria in which at least two members reject the offer, and thus U does not supply group members: as no member is pivotal in that case, they are all indifferent about their recommendation. However, there also exists an equilibrium in which U, being more efficient, keeps supplying all firms. Furthermore, in any such equilibrium, U enters again into *bilaterally efficient* contracts, which leads it to supply the competitive quantity  $q^C$  to all firms; the introduction of a buyer group thus does not affect the equilibrium outputs, but alters the bargaining power of the group members who, by vetoing U's offers, can now secure  $\pi^s (Q_o, \hat{c}) = \pi^s ((n-s) q^C, \hat{c})$ :

**Proposition 3** There exists an equilibrium in which U supplies all firms. Furthermore, under passive conjectures, then in any such equilibrium:

- (i) all firms sell the competitive quantity  $q^C$ ;
- (ii) each non-member earns  $\hat{\pi}^1 = \hat{\pi}$ , whereas each group member earns

$$\hat{\pi}^s \equiv \pi^s \left( (n-s) \, q^C, \hat{c} \right).$$

**Proof.** See Appendix B. ■

Thus, in equilibrium, U ends up supplying the Cournot quantity to all firms, whether they belong to the buyer group or not. Forming a buyer group however affects the division of profits. While non-member firms still earn  $\hat{\pi}$ , group members earn instead  $\hat{\pi}^s$ . Vetoing U's offers to the group not only inflicts a larger loss on U, since U is then delisted as well by the other group members, but it also leads to a situation which, although group members must then rely on less efficient suppliers, is not as bad for the vetoing firm as if it were the only one in that position. As a result, group members benefit from enhanced bargaining power, and the more so, the bigger the group G:

**Proposition 4**  $\hat{\pi} = \hat{\pi}^1 \leq \hat{\pi}^2 \leq ... \leq \hat{\pi}^n < \pi^C$ ; furthermore, for s > 1,  $\hat{\pi}^s > \hat{\pi}^{s-1}$ whenever  $\hat{\pi}^s > 0$  (i.e., whenever  $P((n-s)q^C) > \hat{c}$ ).

#### **Proof.** See Appendix C. ■

As mentioned above, the key intuition here is that, by joining forces in their negotiation with the leading supplier, group members enhance their outside option: while turning to less efficient suppliers remains costly, it becomes less painful when the other members have to do the same. Conversely, alternative decision rules, which do not necessarily grant veto power to a group member, are less effective in enhancing that member's bargaining power, since they do not guarantee that the member will be "in good company" if it rejects U's offer.<sup>14</sup>

<sup>&</sup>lt;sup>14</sup>Suppose for example that U's offers are accepted by G as long as p < s members recommend acceptance; even if each member remains individually free to reject the offer received from U, there

### 4 Discussion and extensions

There is strength in numbers here: relying on less efficient suppliers becomes less and less costly when other firms have to do so as well. For that reason, joining a group not only benefits the additional member, but also benefits the existing group members. In the absence of any restriction on the size of the group, we would thus expect all firms to join the buyer group.

Also, while for the sake of presentation we focused on a single buyer group, the analysis applies as well to situations where several (separate) groups are formed: the members of a group of size s then all earn  $\hat{\pi}^s$ . Still, in the absence of any restriction on group size, we would expect the firms to form a single, encompassing buyer group. Indeed, prospective members benefit more from joining a larger group  $(s' > s \text{ implies } \hat{\pi}^{s'+1} - \hat{\pi} > \hat{\pi}^{s+1} - \hat{\pi})$ , and any existing group member benefits as well from switching to a larger group  $(s' \ge s \text{ implies } \hat{\pi}^{s'+1} > \hat{\pi}^s)$ .

Furthermore, while we focused on a homogenous final good, the analysis applies as well to downstream competitors that are differentiated. In this case, closer competitors are more likely to join forces in their negotiations with the leading supplier. Since the introduction of a buyer group does not affect the equilibrium outputs, the key intuition still refers to group members' outside option: while turning to less efficient suppliers remains costly, it is less painful when the other members who have to do the same are the ones that offer the closest substitutes. To illustrate this point, suppose for instance that the downstream market consists of a differentiated four-firm Cournot oligopoly, where  $D_1$  and  $D_2$  produce the same (good A), whereas  $D_3$  and  $D_4$  produce an imperfect substitute (good B). We thus have:

$$p_1 = p_2 = \hat{P}(Q_A, Q_B)$$
 and  $p_3 = p_4 = \hat{P}(Q_B, Q_A)$ ,

where  $Q_A = q_1 + q_2$  and  $Q_B = q_3 + q_4$ . For the sake of exposition, assume further that the inverse demand  $\hat{P}$  is linear and given by:

$$\hat{P}\left(Q_A, Q_B\right) = 1 - Q_A - \sigma Q_B,$$

then exists equilibria in which U supplies  $q^C$  but leaves only  $\hat{\pi}$  to each and every firm, within as well as without the group (indeed, if p+1 members recommend acceptance, no member is pivotal, and thus belonging to the buyer group makes no difference).

where  $0 \leq \sigma < 1$ . Suppose moreover that c and  $\hat{c}$  satisfy c = 0 and  $\hat{\pi} = \hat{\pi}^1(\hat{c}, 0) > 0$ , which amounts to  $\hat{c} < \frac{2}{3+2\sigma}$ . In the absence of any buyer group, each  $D_i$  sells the competitive quantity  $q^C = \frac{1}{3+2\sigma}$  and earns  $\hat{\pi} = \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{2}\right)^2$ . Suppose now that  $D_1$ and  $D_2$  (who produce perfect substitutes) join forces in their negotiations with U. The equilibrium quantities do not change, but these two firms now each secure a larger profit,  $\hat{\pi}^{12} \equiv \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{3}\right)^2$ . If instead it is  $D_1$  and  $D_3$ , which produce imperfect substitutes, that join forces, the equilibrium quantities remain the same but these firms now each gain  $\hat{\pi}^{13} \equiv \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{2+\sigma}\right)^2 < \hat{\pi}^{12}.^{15}$  Thus, for any  $\sigma < 1$ , it is more profitable for  $D_1$  and  $D_2$ to join forces rather than for  $D_1$  and  $D_3$  (see Appendix D).

In the same vein, we developed these insights in a context with Cournot downstream competition, where output decisions are strategic substitutes, but similar insights apply to other types of downstream competition, such as Bertrand competition with differentiated products, where retail prices are strategic complements: as shown by O'Brien and Shaffer (1992), secret contracting leads again the upstream supplier to offer non-linear tariffs with cost-based marginal wholesale prices, so that the final prices and quantities are again "competitive" (that is, the equilibrium outcome is similar to the one of an *n*-firms oligopoly in which all firms could produce with the same unit cost c). As above, joining a group enhances the outside option of a firm: it does not affect the behavior of the outsiders, but the other group members become weaker rivals when one member exerts its veto power.

Finally, we have assumed so far that contract offers are secret even within the group. This can be justified by the fact that, even if contract offers were communicated to the group, U could then replace them through secret bilateral negotiations with group members.<sup>16</sup> Making these offers observed by all group members – but not by outsiders – would not remove the above-described benefit of joining a group – this would still enhance members' outside options, as above – but would generate an additional strategic effect: in essence, it would eliminate the scope for supplier opportunism within the group, leading the group members to behave as a "cartel". Hence, contrary to the case where

<sup>&</sup>lt;sup>15</sup>Note that, for  $\sigma = 0$ ,  $D_1$  and  $D_3$  do not benefit from joining forces  $(\hat{\pi}^{13} = \hat{\pi})$ , as they do not compete in the same market.

<sup>&</sup>lt;sup>16</sup>Public contracts can have commitment power if renegotiations are constrained, e.g. by agency problems such as adverse selection between the contracting parties. However, as pointed out by Caillaud *et al.* (1995), this is made possible when the parties wish to pre-commit themselves to be more aggressive than they would otherwise. As here U and the group members wish instead to attenuate the competition among themselves, public contracts have no bite if secret renegotiations are feasible.

negotiations remain secret within the group, buyer groups would now have an impact on the equilibrium outcome, and would hurt consumers as well as society. The impact of this additional strategic effect on group members depends on the nature of downstream competition. In case where downstream decisions are strategic complements, as is often the case with Bertrand competition,<sup>17</sup> this would tend to make outsiders "softer", thus reinforcing the incentives to join a group. By contrast, when downstream decisions are strategic substitutes, as is often the case with Cournot competition, this strategic effect is negative. The dynamics of group formation are then less clear-cut. On the one hand, group members become weaker competitors, on the other hand outsiders become tougher competitors. In the same way that a merger benefits outsiders more than it benefit insiders, and may even make them worse-off, a firm may prefer remaining outside the group rather than joining it. Yet, forming a large enough group would still enhance its members' outside option, compared with what they would obtain in the absence of any group (in particular, forming an encompassing group that includes all retailers would remain profitable).

# 5 Upstream investment incentives

An often-voiced concern raised by buyer power relates to its impact on suppliers' incentives to invest and innovate. To explore this issue, we now introduce investment decisions in our framework. More precisely, we add here an additional stage (step 0) at the beginning of the above competition game, in which the dominant supplier, U, can invest F in order to reduce its marginal cost c, from some initial level  $\bar{c} > 0$  to a lower level  $\underline{c} \in [0, \overline{c}]$ . In this extended framework, we study the impact of the size of the buyer group (established before the beginning of the game) on U's equilibrium investment decision. Introducing explicitly U's cost c as an argument in the abovedefined functions, we will denote by  $q^{C}(c)$  and  $\pi^{C}(c)$  the individual quantity and profit in a Cournot equilibrium based on cost c, by  $\Pi^{C}(c)$  the corresponding industry profit, and by  $\hat{\pi}^{s}(\hat{c}, c) = \pi^{s}((n-s)q^{C}(c), \hat{c})$  the outside option (and equilibrium profit) of a member of a buyer group of size s. Note that, by construction,  $q^{n}(0, \hat{c}) = q^{C}(\hat{c})$  and  $\hat{\pi}^{n}(\hat{c}, c) = \pi^{C}(\hat{c})$ ; thus, Lemma 2 implies  $q^{C}(c), \pi^{C}(c) > 0$  if and only c < P(0), in

<sup>&</sup>lt;sup>17</sup>See Vives (1999) for a characterization of the conditions under which firms' decisions are strategic complements or substitutes, for both Bertrand and Cournot competition.

which case  $dq^C/dc, d\pi^C/dc < 0$ .

Obviously, it is socially or privately interesting to invest only when this allows U to be the most effective supplier (i.e.,  $\underline{c} < \hat{c}$ , P(0)). The incentives to invest however also depend on whether the competitive fringe, too, is an effective supplier ( $\hat{c} \ge P(0)$ ), as well as on whether U is initially more efficient than the fringe ( $\overline{c} \ge \hat{c}$ ). More precisely, in equilibrium U supplies the retailers whenever it is more efficient than the fringe, that is, whenever its cost c is lower than  $\hat{c}$ ; we will therefore let

$$\Pi_I(c) \equiv \Pi^C(\min\{c, \hat{c}\})$$

denote the industry profit, as a function of U's cost c, and

$$\Delta_I = \Pi_I \left(\underline{c}\right) - \Pi_I \left(\overline{c}\right)$$

denote the investment benefit for the industry. Similarly, since a member of a buyer group of size s obtains a profit equal to  $\hat{\pi}^s(\hat{c}, \min\{c, \hat{c}\})$  when U's cost is c, U's profit can then be written as

$$\Pi_{U}^{s}(c) \equiv \Pi_{I}(c) - s\hat{\pi}^{s}(\hat{c}, \min\{c, \hat{c}\}) - (n-s)\hat{\pi}^{1}(\hat{c}, \min\{c, \hat{c}\}),$$

and its incentive to invest is driven by a private benefit equal to

$$\Delta_U^s = \Pi_U^s \left(\underline{c}\right) - \Pi_U^s \left(\overline{c}\right).$$

Investing is neither privately nor socially desirable (that is,  $\Delta_U^s = \Delta_I = 0$ ) when  $\hat{c} < \underline{c}$ , since it does not allow U to become a viable supplier in that case. Conversely, when the competitive fringe does not offer a viable option (i.e., when  $\hat{c} \ge P\left((n-s) q^C(\overline{c})\right)$ ), retailers obtain zero profit whether there is a buyer group or not; this leads U to fully internalize the impact of its investment on the industry profit and thus aligns its incentives with that of the industry (that is,  $\Delta_U^s = \Delta_I$ ). The same applies when retailers form an encompassing group (i.e., s = n), since they then earn a profit equal to  $\Pi^C(\hat{c})$ , regardless of U's cost; therefore, U fully internalizes again the impact of its on the industry profit, and  $\Delta_U^n = \Delta_I$ .

In all other cases (that is, when s < n and  $\underline{c} < \hat{c} < P((n-s)q^C(\overline{c}))$ ), by investing

U increases its profit not only by lowering its cost, but also possibly by limiting the value of retailers' outside option, if they were to turn to the fringe suppliers; indeed, we then have:

$$\Delta_U^s - \Delta_I = s \left[ \hat{\pi}^s \left( \hat{c}, \min\left\{ \overline{c}, \hat{c} \right\} \right) - \hat{\pi}^s \left( \hat{c}, \underline{c} \right) \right] + (n-s) \left[ \hat{\pi}^1 \left( \hat{c}, \min\left\{ \overline{c}, \hat{c} \right\} \right) - \hat{\pi}^1 \left( \hat{c}, \underline{c} \right) \right],$$
(2)

where the terms in brackets are non-negative (and the first one is positive) since  $\hat{\pi}^k(\hat{c}, c)$ weakly increases with c (and strictly so for k = s) from  $\underline{c}$  to min  $\{\overline{c}, \hat{c}\}$ . As a result, Uhas excessive incentives to invest, compared with what would maximize industry profits (that is,  $\Delta_U^s > \Delta_I$ ):

**Proposition 5**  $\Delta_U^s \ge \Delta_I$  for any  $\overline{c} > \underline{c} \ge 0$ , any  $\hat{c} \ge 0$  and any  $s \in \{1, ..., n\}$ ; more precisely:

(i)  $\Delta_U^s = \Delta_I \text{ if } \hat{c} < \underline{c}, \ \hat{c} \ge P\left((n-s) q^C(\overline{c})\right), \text{ or } s = n;$ (ii)  $\Delta_U^s > \Delta_I \text{ if instead } s < n \text{ and } \underline{c} < \hat{c} < P\left((n-s) q^C(\overline{c})\right).$ 

#### **Proof.** See Appendix E.

Reducing retailers' rents thus gives U an additional motive for investing in cost reduction, which tends to increase its incentives to invest, beyond what would maximize industry profitability. We now show that, while creating or expanding a buyer group increases retailers' profit at the expanse of U, the impact on U's incentives to invest is however ambiguous. For example, when  $\hat{c} \geq P\left(q^{C}(\bar{c})\right)$ , the formation of a buyer group either has no effect (as long as s < n, since then  $\hat{\pi}^s(\hat{c}, \overline{c}) = \hat{\pi}^s(\hat{c}, \underline{c}) = 0$ ), or reduces U's rent by  $\Pi^{C}(\hat{c})$ , regardless of U's cost (if s = n). Thus, while the creation or the expansion of a buyer group can reduce U's rent (if s = n), it never affects U's investment incentives in that case  $(\Delta_U^s = \Delta_I \text{ for any } s \leq n)$ . When instead  $\hat{c} < P(q^C(\overline{c}))$ , setting-up a large enough group (i.e., s close enough to n) allows retailers to obtain a positive profit, and expanding it further moreover tends to make retailers' outside option less sensitive to U's cost, at it reduces the number of retailers that rely on U in this alternative scenario, and thus tends to eliminate the scope for overinvestment; thus, for s large enough, we expect  $\Delta_U^s$  to decrease as s further increases, and eventually converge towards  $\Delta_I$ . When instead the buyer group is initially small, expanding its size strengthens retailers' weak bargaining position, and may well do so more effectively when U is itself not too strong; this, in turn, may reinforce U's incentives to invest in cost reduction; for example, if  $\hat{\pi}^s(\hat{c}, \overline{c}) > \hat{\pi}^s(\hat{c}, \underline{c}) = 0$ , then U clearly has an extra incentive to invest when a buyer group of size s has formed, so as to prevent retailers from gaining any bargaining power, and thus  $\Delta_U^s > \Delta_I$ . The following Proposition reflects this intuition:

**Proposition 6** For any  $\overline{c} > \underline{c} \ge 0$  and any s < n: (1)  $\Delta_U^{s+1} = \Delta_U^s$  if  $\hat{c} \le \underline{c}$  or  $\hat{c} \ge P(q^C(\overline{c}))$ ; (2) if instead  $\underline{c} < \hat{c} < P(q^C(\overline{c}))$ :

(i)  $\Delta_U^{s+1} < \Delta_U^s$  for s large enough;

(ii) however, if  $\hat{c} \geq P((n-1)q^C(\overline{c}))$ , then  $\Delta_U^{s+1} \geq \Delta_U^s$  for s not too large, with at least one strict inequality in that range.

### **Proof.** See Appendix F.1.

Setting-up of expanding a buyer group may thus *foster* U's incentives to invest if the group is not too large, and tends instead to counterbalance the overinvestment bias, and reduce investment incentives, when the group is large. To illustrate this proposition, suppose for example that the costs  $\hat{c}, \bar{c}, \bar{c}$  satisfy  $\hat{c} > \bar{c} > \bar{c}$ ,  $\pi^C(\hat{c}) > 0$ , and  $\hat{\pi}^1(\hat{c}, \bar{c}) =$  $\hat{\pi}^1(\hat{c}, \underline{c}) = 0$ . There then exists  $\bar{s}$  and  $\underline{s} \geq \bar{s}$  such that  $\hat{\pi}^s(\hat{c}, \bar{c}) > 0$  (resp.,  $\hat{\pi}^s(\hat{c}, \underline{c}) > 0$ ) if and only if  $s \geq \bar{s}$  (resp.,  $s \geq \underline{s}$ ). We then have (Figure 1 provides an illustration for  $n = 10, P(Q) = 1 - q, \hat{c} = 0.7, \bar{c} = 0.45, \text{ and } \underline{c} = 0$ ; see Appendix F.2 for a detailed analysis of this case):

- in the range  $s < \bar{s}$ ,  $\hat{\pi}^s(\hat{c}, \bar{c}) = \hat{\pi}^s(\hat{c}, \underline{c}) = 0$ , and thus  $\Delta_U^s = \Delta_I$ ;
- in the range  $\bar{s} \leq s < \underline{s}$ ,  $\hat{\pi}^s(\hat{c}, \underline{c}) = 0$  but  $\hat{\pi}^s(\hat{c}, \overline{c})$  is positive and increases with s; as a result, U has more incentives to invest than what would maximize industry profits  $(\Delta_U^s > \Delta_I)$ , and the more so, the larger the buyer group:  $\Delta_U^s$  increases as s increases;
- finally, in the range  $s > \underline{s}$ ,  $\hat{\pi}^s(\hat{c}, \overline{c})$  and  $\hat{\pi}^s(\hat{c}, \underline{c})$  are both positive and increasing in s. While  $\hat{\pi}^s(\hat{c}, \underline{c})$  remains smaller than  $\hat{\pi}^s(\hat{c}, \overline{c})$  as s increases, it first increases more slowly, and then more quickly than  $\hat{\pi}^s(\hat{c}, \overline{c})$  (and the two coincide with  $\pi^C(\hat{c})$ for s = n); as a result,  $\Delta_U^s$  first increases and then decreases as s increases (and finally coincides again with  $\Delta_I$  for s = n).

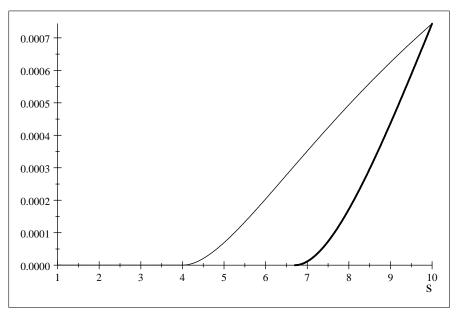


Figure 1a: Retailers' profits  $(\hat{\pi}^{s}(\hat{c},\underline{c}) - \text{in bold} - \text{and } \hat{\pi}^{s}(\hat{c},\overline{c}))$ 

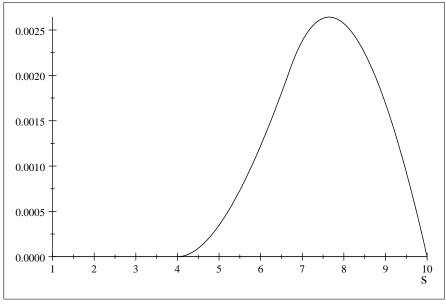


Figure 1b: Investment incentives  $(\Delta^s_U)$ 

Remark: implications for group formation. The above analysis shows that

forming a group affect U's investment incentives, as well as the value of group members' outside option. More precisely: (i) keeping constant the investment level, downstream firms are always willing to join as large a group as possible, as this enhances their bargaining position, and thus their equilibrium profit; and (ii) keeping constant the size of the group, the value of this outside option decreases as U's invests more. As increasing the size of the group eventually decreases U's investment incentives – back to the level  $(\Delta_I)$  that would prevail absent a buyer group –, it follows that, in order to maximize the value of their equilibrium profit, downstream firms still have an incentive to join as large a group as possible: this minimizes U's investment incentives (as  $\Delta_I \leq \Delta_U^s$  for any size s), and moreover maximizes their bargaining position, given this investment level.

### 6 Conclusion

While the literature on buyer power has mainly studied the impact of retail mergers, in this paper we focus instead on the bargaining power that *buyer groups* confer to firms that are and remain competitors in the same retail market. We show that, by joining forces in their procurement negotiations, downstream firms can enhance their bargaining position at the expense of their suppliers. They can do so by creating a buyer group that selects suppliers on behalf of its members, in which each group member can veto an offer, in which case all group members must turn to alternative suppliers. Transforming individual listing decisions into a joint listing decision makes delisting less harmful, which in turn improves group members' bargaining position compared to outsiders.

In our framework, where secret contracting implies that contracts are bilaterally efficient, the enhanced bargaining position conferred by buyer groups does not lead to lower prices for consumers. This is in line with a concern often voiced by antitrust authorities: cost savings resulting from joint purchasing arrangement are not necessarily passed on to consumers. However, by contrast to another concern of antitrust authorities, the formation of buyer groups has no impact here on other purchasers: the equilibrium contracts are bilaterally efficient and their outside options are unchanged.

We also show that this additional buyer power can have an ambiguous impact on a supplier's incentives to invest: enlarging a buyer group may foster its incentives to invest if the group is not too large, and tends instead to counterbalance overinvestment biases, and reduce investment incentives, when the group is already quite large. The source of buyer power that we identify originates directly from the competition in retail markets. While for the sake of presentation we focused on a buyer group only composed of firms that compete in the same downstream market, the analysis applies as well to hybrid buyer groups, where some members are on separate markets while others compete in the same market. It is however the presence of competition in the group that enhances a given member's bargaining position. Thus, prospective members benefit more from joining a group in which the number of direct competitors is the largest. Similarly, it is the closest competitors that gain most from joining forces in their negotiations with suppliers.

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# Appendix

## A Proof of Lemma 2

The following Lemma will be useful:

**Lemma 7** Under Assumption 1, for any  $k \in \mathbb{N}^*$  and any Q and q satisfying  $Q \ge q \ge 0$ , kP'(Q) + P''(Q) q < 0.

**Proof.** Since P'(Q) < 0, the expression kP'(Q) + P''(Q)q is negative whenever  $P''(Q) \leq 0$ ; if instead P''(Q) > 0, then Assumption 1, together with P'(Q) < 0 and  $q \leq Q$ , yields

$$kP'(Q) + P''(Q)q \le P'(Q) + P''(Q)Q < 0.$$

Assumption 1 ensures that each group member's profit is strictly concave in its own quantity: letting  $q_i$  denote the member's output,  $Q_{-i} = Q_o + \sum_{j \in S \setminus \{i\}}$  its rivals' aggregate output and  $Q = Q_{-i} + q_i$  the total output, we have

$$\frac{\partial^2 \pi\left(q_i; Q_{-i}, \hat{c}\right)}{\partial q_i^2} = 2P'\left(Q\right) + P''\left(Q\right)q_i < 0,$$

where the inequality stems from Lemma 7. Furthermore, the first-order derivative of the member's profit is:

$$\frac{\partial \pi\left(q_{i};Q_{-i},\hat{c}\right)}{\partial q_{i}}\bigg|_{q_{i}=0}=P\left(Q\right)-\hat{c}.$$

Therefore, if  $P(Q) \leq \hat{c}$ , then all group members choose  $q_i = 0$ , in which case  $Q = Q_o$ and thus  $P(Q_o) \leq \hat{c}$ ; conversely, if  $P(Q_o) \leq \hat{c}$ , so that  $P(Q) < \hat{c}$  for any  $Q > Q_o$ , each member necessarily chooses  $q_i = 0$ , which satisfies (1).

When instead  $P(Q) > \hat{c}$ , each group member must choose a positive quantity  $q_i > 0$ , thus satisfying the first-order condition

$$P\left(Q\right) + P'\left(Q\right)q_i = \hat{c}.$$

If follows that  $q_i = q^s$  (i.e., all members must choose the same quantity),<sup>18</sup> where  $q^s > 0$  thus satisfies (1) or, equivalently, the first-order condition

$$P(sq^{s} + Q_{o}) + P'(sq^{s} + Q_{o})q^{s} = \hat{c}.$$
(3)

Let  $Q^s \equiv sq^s + Q_o$  denote the aggregate equilibrium output. Differentiating (3) with respect to  $\hat{c}$ ,  $Q_o$  and  $q^s$  yields:

$$\begin{array}{lll} \frac{\partial q^{s}}{\partial \hat{c}} & = & \frac{1}{\left(s+1\right)P'\left(Q^{s}\right)+P''\left(Q^{s}\right)sq^{s}} < 0, \\ \frac{\partial q^{s}}{\partial Q_{o}} & = & -\frac{P'\left(Q^{s}\right)+P''\left(Q^{s}\right)q^{s}}{\left(s+1\right)P'\left(Q^{s}\right)+P''\left(Q^{s}\right)sq^{s}} < 0, \end{array}$$

where the inequalities follow from Lemma 7.

We now turn to  $\pi^s$ . Using  $\pi^s = \max_{q_i} \pi(q_i; Q_o + (s-1)q^s, \hat{c})$  and the envelope theorem, we have:

$$\begin{aligned} \frac{\partial \pi^{s}}{\partial \hat{c}} &= \left. \frac{\partial \pi \left( q_{i}; Q_{-i}, \hat{c} \right)}{\partial Q_{-i}} \right|_{q_{i}=q^{s}, Q=Q^{s}} \left( s-1 \right) \frac{\partial q^{s}}{\partial \hat{c}} + \left. \frac{\partial \pi \left( q_{i}; Q_{-i}, \hat{c} \right)}{\partial \hat{c}} \right|_{q_{i}=q^{s}, Q=Q^{s}} \\ &= \left. P' \left( Q^{s} \right) q^{s} \left( s-1 \right) \frac{\partial q^{s}}{\partial \hat{c}} - q^{s} \\ &= \left[ \frac{\left( s-1 \right) P' \left( Q^{s} \right)}{\left( s+1 \right) P' \left( Q^{s} \right) + P'' \left( Q^{s} \right) sq^{s}} - 1 \right] q^{s} \\ &= \left. - \frac{2P' \left( Q^{s} \right) + P'' \left( Q^{s} \right) sq^{s}}{\left( s+1 \right) P' \left( Q^{s} \right) + P'' \left( Q^{s} \right) sq^{s}} q^{s} < 0, \end{aligned}$$

<sup>&</sup>lt;sup>18</sup>This is a common feature of aggregative games, where one player's objective depends on others' decisions only through an aggregator (here, total output) of all individual decisions. See Anderson, Erkal and Piccinin (2011) for a recent treatment of such games.

where the inequality follows again from Lemma 7. The envelope theorem yields similarly:

$$\begin{aligned} \frac{\partial \pi^{s}}{\partial Q_{o}} &= \left. \frac{\partial \pi \left( q_{i}; Q_{-i}, \hat{c} \right)}{\partial Q_{-i}} \right|_{q_{i}=q^{s}, Q=Q^{s}} \left( 1 + \left( s - 1 \right) \frac{\partial q^{s}}{\partial Q_{o}} \right) \\ &= \left. P' \left( Q^{s} \right) q^{s} \left( 1 + \left( s - 1 \right) \frac{\partial q^{s}}{\partial Q_{o}} \right) \right. \\ &= \left. P' \left( Q^{s} \right) q^{s} \frac{2P' \left( Q^{s} \right) + P'' \left( Q^{s} \right) q^{s}}{\left( s + 1 \right) P' \left( Q^{s} \right) + P'' \left( Q^{s} \right) sq^{s}} < 0, \end{aligned}$$

where the inequality follows again from P'(Q) < 0 and Lemma 7.

### **B** Proof of Proposition 3

Consider a candidate equilibrium in which: (i) U supplies all firms, which implies that all group members recommend accepting U's offers, and (ii)  $q_i \neq R^C(Q_{-i}; c)$  for some downstream firm  $D_i$ , where  $Q_{-i}$  denotes the aggregate equilibrium output of  $D_i$ 's rivals.  $D_i$ 's equilibrium profit, of the form  $\pi_i = P(Q_{-i} + q_i + \hat{q}_i)(q_i + \hat{q}_i) - T_i - \hat{c}\hat{q}_i$ , must satisfy  $\pi_i \geq \hat{\pi}_i$ , where  $\hat{\pi}_i$  represents the profit that  $D_i$  can obtain with its relevant outside option:  $\hat{\pi}_i = \pi^1(Q_{-i}, \hat{c})$  if  $D_i$  does not belong to the buyer group G, whereas  $\hat{\pi}_i = \pi^s(Q_o, \hat{c})$  otherwise, where  $Q_o$  denotes the aggregate equilibrium output of firms outside G. Moreover, the constraint  $\pi_i \geq \hat{\pi}_i$  must be binding; otherwise, U could deviate and slightly increase the payment  $T_i$ : under passive conjectures,  $D_i$  would still accept (or, if belonging to G, would still recommend acceptance, leading G to accept U's offers), and the deviation would thus increase U's profit. Therefore, we must have  $\pi_i = \hat{\pi}_i$ .

Suppose now that U deviates and offers  $D_i$  to supply  $\tilde{q}_i = R^C(Q_{-i}; c)$  for some total price  $\tilde{T}_i$ . Under passive conjectures,  $D_i$  anticipates its rivals to stick to their equilibrium outputs, and (other) group members to keep recommending acceptance of U's offers to the group. It follows that, if  $D_i$  accepts the offer, the impact of this deviation on the

joint profits of U and  $D_i$  is given by:

$$\begin{cases} \left[\tilde{T}_{i} - c\tilde{q}_{i}\right] + \max_{q \ge 0} \left[P\left(Q_{-i} + \tilde{q}_{i}\right)\left(\tilde{q}_{i} + q\right) - \tilde{T}_{i} - \hat{c}q\right] \\ \\ - \left\{\left[T_{i} - cq_{i}\right] + \left[P\left(Q_{-i} + q_{i} + \hat{q}_{i}\right)\left(q_{i} + \hat{q}_{i}\right) - T_{i} - \hat{c}\hat{q}_{i}\right] \right\} \\ \\ \ge \left\{\left[\tilde{T}_{i} - c\tilde{q}_{i}\right] + \left[P\left(Q_{-i} + \tilde{q}_{i}\right)\tilde{q}_{i} - \tilde{T}_{i}\right] \right\} - \left\{\left[T_{i} - cq_{i}\right] + \left[P\left(Q_{-i} + q_{i} + \hat{q}_{i}\right)\left(q_{i} + \hat{q}_{i}\right) - T_{i} - \hat{c}\hat{q}_{i}\right] \right\} \\ \\ = \left(P\left(Q_{-i} + \tilde{q}_{i}\right) - c\right)\tilde{q}_{i} - \left\{\left(P\left(Q_{-i} + q_{i} + \hat{q}_{i}\right) - c\right)\left(q_{i} + \hat{q}_{i}\right) - \left(\hat{c} - c\right)\hat{q}_{i} \right\}. \end{cases}$$

The last expression is positive since  $(P(Q_{-i} + \tilde{q}_i) - c)\tilde{q}_i = \max_{\tilde{q} \ge 0} (P(Q_{-i} + \tilde{q}) - c)\tilde{q}$ and:

• if  $\hat{q}_i = 0$ , then  $q_i + \hat{q}_i = q_i \neq R^C(Q_{-i}; c)$  implies

$$(P(Q_{-i} + q_i + \hat{q}_i) - c)(q_i + \hat{q}_i) < \max_{\tilde{q} \ge 0} (P(Q_{-i} + \tilde{q}) - c)\tilde{q};$$

• if  $\hat{q}_i > 0$ , then:

$$(P(Q_{-i} + q_i + \hat{q}_i) - c)(q_i + \hat{q}_i) - (\hat{c} - c)\hat{q}_i < (P(Q_{-i} + q_i + \hat{q}_i) - c)(q_i + \hat{q}_i) \leq \max_{\tilde{q} \ge 0} (P(Q_{-i} + \tilde{q}) - c)\tilde{q}.$$

Therefore, in both cases the deviating offer increases the joint profit of U and  $D_i$  if it is accepted; there thus exists a price  $\tilde{T}_i$  that is mutually profitable, i.e., that gives  $D_i$  more than  $\pi_i = \hat{\pi}_i$  (so that U's offer is indeed accepted, either individually or by the group) and yet increases U's profit.

Therefore, any equilibrium in which U supplies all firms, and firms have passive conjectures, must be such that  $q_i = R^C(Q_{-i};c)$  for i = 1, ..., n; this, in turn, implies  $q_i = q^C$ . It follows that, in any such equilibrium:

- If  $D_i$  does not belong to G, it can secure  $\hat{\pi}_i = \hat{\pi}$  by rejecting U's offer;
- If instead  $D_i$  belongs to G, it can secure  $\hat{\pi}_i = \hat{\pi}^s$  by recommending the rejection of U's offers to the group.

Conversely, suppose that U offers to supply  $q^c$  to each  $D_i$ , for a total payment equal to  $P(nq^C) q^C - \hat{\pi}_i$ , where  $\hat{\pi}_i$  is defined as above. By construction, a deviating offer that

is acceptable by  $D_i$  cannot increase the joint bilateral profit of U and  $D_i$ ; since  $D_i$  can secure  $\hat{\pi}_i$  by rejecting U's offer (or recommending its rejection), such deviation cannot be profitable for U. Obviously, deviating and not supplying a non-member firm  $D_i$  is also unprofitable, as it would reduce U's profit by

$$(P(nq^{C}) - c)q^{C} - \hat{\pi} = \pi^{1}((n-1)q^{C}; c) - \pi^{1}((n-1)q^{C}; \hat{c}) \ge 0.$$

Finally, deviating offers that are rejected by the buyer group G cannot be profitable either, as it would reduce U's profit by

$$s\left[\left(P\left(nq^{C}\right)-c\right)q^{C}-\hat{\pi}^{s}\right]=s\left[\pi^{s}\left(\left(n-s\right)q^{C};c\right)-\pi^{s}\left(\left(n-s\right)q^{C};\hat{c}\right)\right]\geq0.$$

### C Proof of Proposition 4

By construction,  $\hat{\pi} = \pi^1 \left( (n-s) q^C; \hat{c} \right) = \hat{\pi}^1, \ \hat{\pi}^n = \pi^n (0; \hat{c})$  and  $\pi^C = \pi^n (0; c)$ ; furthermore, the latter is positive from Assumption 1 and Lemma 2, which in turn implies  $\pi^C = \pi^n (0; c) > \hat{\pi}^n = \pi^n (0; \hat{c}).$ 

Let  $\hat{q}^s \equiv q^s ((n-s) q^C; \hat{c})$  denote each group member's continuation equilibrium output if the group were to reject U's offers. From Assumption 1 and Lemma 2,  $q^C = q^s ((n-s) q^C; c) > 0$  and:

$$q^{C} = q^{s} \left( (n-s) q^{C}; c \right) > \hat{q}^{s} = q^{s} \left( (n-s) q^{C}; \hat{c} \right)$$

By construction, for s > 1, we have  $\hat{\pi}^{s-1} = \pi^{s-1} \left( (n-s+1) q^C; \hat{c} \right)$  and

$$\hat{\pi}^{s} = \pi^{s-1} \left( (n-s) q^{C} + \hat{q}^{s}; \hat{c} \right).$$

The conclusion then follows from Lemma 2, which implies that the profit function  $\pi^{s}(Q_{o}, \hat{c})$  decreases as the outsiders' output  $Q_{o}$  increases, and does strictly so as long as it remains positive, which is the case if and only if  $P(Q_{o}) > \hat{c}$ .

## **D** Illustration for imperfect substitutes

We study here the differentiated four-firm Cournot oligopoly introduced in section 4, in which  $D_1$  and  $D_2$  produce good A whereas  $D_3$  and  $D_4$  produce good B.

In the absence of any buyer group, each  $D_i$  (i = 1, 2, 3, 4) sells the competitive quantity  $q^C$ , which solves

$$\max_{q} \hat{P}\left(q^{C}+q, 2q^{C}\right)q = \left(1-\left(q^{C}+q\right)-2\sigma q^{C}\right)q.$$

As this profit is concave,  $q^C$  is thus characterized by the first-order condition:<sup>19</sup>

$$0 = 1 - (q^{C} + q) - 2\sigma q^{C} - q\big|_{q=q^{C}} = 1 - (3 + 2\sigma) q^{C},$$

i.e.,

$$q^C = \frac{1}{3+2\sigma}$$

Furthermore, each  $D_i$  earns the profit it could obtain by turning to the competitive fringe:

$$\hat{\pi} = \left(\hat{P}\left(q^{C} + \hat{q}, 2q^{C}\right) - \hat{c}\right)\hat{q} \equiv \max_{q}\left(\hat{P}\left(q^{C} + q, 2q^{C}\right) - \hat{c}\right)q,$$

where

$$\begin{pmatrix} \hat{P}(q^{C}+q,2q^{C})-\hat{c} \end{pmatrix} q = \left(1-(1+2\sigma)q^{C}-q-\hat{c}\right)\hat{q} \\ = \left(1-\frac{1+2\sigma}{3+2\sigma}-q-\hat{c}\right)\hat{q} \\ = \left(\frac{2}{3+2\sigma}-q-\hat{c}\right)q.$$

The profit  $\hat{\pi}$  is positive when  $\hat{c} < \frac{2}{3+2\sigma}$ , in which case  $\hat{q}$  is determined by the first-order condition:

$$\frac{2}{3+2\sigma} - \hat{c} - 2\hat{q} = 0,$$

i.e.,

$$\hat{q} = \frac{1}{3+2\sigma} - \frac{\hat{c}}{2},$$

<sup>19</sup>In what follows,  $\hat{P}_1$  denotes the partial derivative of  $\hat{P}$  with respect to its first argument.

leading to

$$\hat{\pi} = \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{2}\right)^2.$$

Suppose now that  $D_1$  and  $D_2$  form a buyer group. Equilibrium quantities remain the same, and outsiders still earn  $\hat{\pi}$ , but the group members now each secure:

$$\hat{\pi}^{12} = \left(\hat{P}\left(2\hat{q}^{12}, 2q^{C}\right) - \hat{c}\right)\hat{q}^{12} \equiv \max_{q}\left(\hat{P}\left(\hat{q}^{12} + q, 2q^{C}\right) - \hat{c}\right)q,$$

where

$$\begin{pmatrix} \hat{P}(\hat{q}^{12}+q,2q^{C})-\hat{c} \end{pmatrix} q = (1-(\hat{q}^{12}+q)-2\sigma q^{C}-\hat{c})\hat{q} \\ = (1-(\hat{q}^{12}+q)-\frac{2\sigma}{3+2\sigma}-\hat{c})\hat{q} \\ = (\frac{3}{3+2\sigma}-(\hat{q}^{12}+q)-\hat{c})q.$$

The first-order condition yields, for  $q = \hat{q}^{12}$ :

$$\frac{3}{3+2\sigma} - \hat{c} - 3\hat{q}^{12} = 0,$$

i.e.,

$$\hat{q}^{12} = \frac{1}{3+2\sigma} - \frac{\hat{c}}{3},$$

leading to

$$\hat{\pi}^{12} = \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{3}\right)^2.$$

If instead  $D_1$  and  $D_3$  form a buyer group, they each gain:

$$\hat{\pi}^{13} = \left(\hat{P}\left(q^{C} + \hat{q}^{13}, q^{C} + \hat{q}^{13}\right) - \hat{c}\right)\hat{q}^{13} \equiv \max_{q}\left(\hat{P}\left(q^{C} + q, q^{C} + \hat{q}^{13}\right) - \hat{c}\right)q,$$

where

$$\begin{pmatrix} \hat{P}(q^{C}+q,q^{C}+\hat{q}^{13})-\hat{c} \end{pmatrix} q = (1-(q^{C}+q)-\sigma(q^{C}+\hat{q}^{13})-\hat{c})\hat{q} \\ = (1-\frac{1+\sigma}{3+2\sigma}-q-\sigma\hat{q}^{13}-\hat{c})\hat{q} \\ = (\frac{2+\sigma}{3+2\sigma}-q-\sigma\hat{q}^{13}-\hat{c})q.$$

The first-order condition yields, for  $q = \hat{q}^{13}$ :

$$\frac{2+\sigma}{3+2\sigma} - (2+\sigma)\,\hat{q}^{13} - \hat{c} = 0,$$

i.e.,

$$\hat{q}^{13} = \frac{1}{3+2\sigma} - \frac{\hat{c}}{2+\sigma},$$

leading to

$$\hat{\pi}^{13} = \left(\frac{1}{3+2\sigma} - \frac{\hat{c}}{2+\sigma}\right)^2.$$

It is straightforward to check that  $\hat{\pi}^{12} > \hat{\pi}^{13} > \hat{\pi}$ .

## E Proof of Proposition 5

The following Lemma will be useful:

**Lemma 8** For any  $k \in \{1, ..., n-1\}$ , and any  $\hat{c}, c \ge 0$ :

$$\frac{\partial \hat{\pi}^k}{\partial c} \left( \hat{c}, c \right) \ge 0,\tag{4}$$

with a strict inequality whenever c < P(0) (i.e.,  $q^{C}(c) > 0$ ) and  $\hat{c} < P((n-k)q^{C}(c))$ .

**Proof.** We have:

$$\frac{\partial \hat{\pi}^{k}}{\partial c}\left(\hat{c},c\right) = \left.\frac{\partial \pi^{k}}{\partial Q_{o}}\left(Q_{o},\hat{c}\right)\right|_{Q_{o}=(n-k)q^{C}(c)}\left(n-k\right)\frac{dq^{C}}{dc}\left(c\right).$$

The conclusion then follows from Lemma 2, which ensures that  $\frac{\partial \pi^k}{\partial Q_o} (Q_o, \hat{c}) \Big|_{Q_o = (n-k)q^C(c)} \geq 0$ , with a strict inequality whenever  $\hat{c} < P((n-k)q^C(c))$ , and (when applied to the case  $Q_o = 0$  and s = n)  $\frac{dq^C}{dc} \leq 0$ , with a strict inequality whenever c < P(0).

We now consider in turn the various cases discussed in the text:

- When  $\hat{c} < \underline{c}$ , investing is neither privately nor socially desirable, since it does not allow U to become a viable supplier in that case:  $\Delta_U^s = \Delta_I = 0$ .
- When  $\hat{c} \geq P\left((n-s) q^{C}(\bar{c})\right)$ , the competitive fringe does not offer a viable option:  $\hat{\pi}^{s}(\hat{c},c) = 0$ , and thus  $\Pi_{U}^{s}(c) = \Pi_{I}(c)$ , for both  $c = \min\{\underline{c},\hat{c}\}$  and  $c = \min\{\overline{c},\hat{c}\}$ ; therefore, U fully internalize the impact of its investment on the industry profit:  $\Delta_{U}^{s} = \Delta_{I}$ .
- When s = n, retailers earn a profit equal to  $\hat{\pi}^n(\hat{c}, c) = \Pi^C(\hat{c})$ , regardless of U's cost c; this leads again U to fully internalize the impact of its on the industry profit:  $\Delta_U^s = \Delta_I$ .

Consider now the case where s < n and  $\underline{c} < \hat{c} < P\left((n-s) q^{C}(\overline{c})\right)$ . Since  $\min \{\underline{c}, \hat{c}\} = \underline{c}$ ,  $\Delta_{U}^{s} - \Delta_{I}$  is indeed given by (2), and moreover  $\min \{\underline{c}, \hat{c}\} = \underline{c} < \min \{\overline{c}, \hat{c}\}$ . Lemma 8 then implies that the terms in brackets,  $\hat{\pi}^{s}(\hat{c}, \min \{\overline{c}, \hat{c}\}) - \hat{\pi}^{s}(\hat{c}, \underline{c})$  and  $\hat{\pi}^{1}(\hat{c}, \min \{\overline{c}, \hat{c}\}) - \hat{\pi}^{1}(\hat{c}, \underline{c})$ , are both non-negative. The first term is moreover positive, since  $\frac{\partial \hat{\pi}^{s}}{\partial c}(\hat{c}, c)|_{c=\min\{\overline{c}, \hat{c}\}} > 0$ :

- If  $\hat{c} \leq \bar{c}$ ,  $\hat{\pi}^s(\hat{c}, \min\{\bar{c}, \hat{c}\}) = \hat{\pi}^s(\hat{c}, \hat{c}) = \pi^C(\hat{c})$ , and  $\hat{c} < P\left((n-s)q^C(\bar{c})\right) (\leq P(0))$ implies  $\hat{c} < P(0)$ , which in turn implies  $\pi^C(\hat{c}) > 0$  and thus  $\hat{c} < \left(P\left(nq^C(\hat{c})\right) < \right)P\left((n-s)q^C(\hat{c})\right)$ therefore, from Lemma 8,  $\frac{\partial \hat{\pi}^s}{\partial c}(\hat{c}, c)\Big|_{c=\hat{c}} > 0$ .
- If  $\hat{c} > \overline{c}$ ,  $\hat{\pi}^s(\hat{c}, \min\{\overline{c}, \hat{c}\}) = \hat{\pi}^s(\hat{c}, \overline{c}); \ \hat{c} < P((n-s)q^C(\overline{c}))$  then implies  $\overline{c} < (\hat{c} < P((n-s)q^C(\overline{c})) <) P(0)$ , and thus from Lemma 8,  $\frac{\partial \hat{\pi}^s}{\partial c}(\hat{c}, c)|_{c=\overline{c}} > 0$ .

The conclusion follows.

### **F** Upstream investment incentives

### F.1 Proof of Proposition 6

Consider first the case  $\hat{c} \ge P\left(q^C\left(\overline{c}\right)\right) (\ge P\left(q^C\left(\underline{c}\right)\right))$ .

- For any s < n,  $\hat{\pi}^s(\hat{c}, \overline{c}) = \hat{\pi}^s(\hat{c}, \underline{c}) (= 0)$ ; therefore:
  - if  $q^{C}(\overline{c}) > 0$ , then  $P(q^{C}(\overline{c})) > \overline{c}$ ;  $\hat{c} \ge P(q^{C}(\overline{c}))$  thus implies  $\hat{c} > \overline{c} > \underline{c}$ , and we have:  $\hat{\pi}^{s}(\hat{c}, \min\{\overline{c}, \hat{c}\}) (= \hat{\pi}^{s}(\hat{c}, \overline{c})) = \hat{\pi}^{s}(\hat{c}, \min\{\underline{c}, \hat{c}\}) (= \hat{\pi}^{s}(\hat{c}, \underline{c})) = 0$ , and thus  $\Delta_{U}^{s} = \Delta_{I}$ ;
  - if  $q^{C}(\overline{c}) = 0$ , then  $\hat{c} \geq P(q^{C}(\overline{c})) = P(0)$  implies that  $\hat{c}$  is never a viable option (even when outsiders are also supplied at  $\hat{c}$ ), and thus again  $\hat{\pi}^{s}(\hat{c}, \min{\{\overline{c}, \widehat{c}\}}) = \hat{\pi}^{s}(\hat{c}, \min{\{\underline{c}, \widehat{c}\}}) = 0$ , and  $\Delta_{U}^{s} = \Delta_{I}$ .
- For s = n, we also have  $\hat{\pi}^n(\hat{c}, \min\{\overline{c}, \hat{c}\}) = \hat{\pi}^n(\hat{c}, \min\{\underline{c}, \hat{c}\}) (= \pi^C(\hat{c}))$ , and thus  $\Delta_U^s = \Delta_I$ .

Therefore, for any  $s \in \{1, ..., n\}$ ,  $\Delta_U^s = \Delta_I$ ; thus,  $\Delta_U^{s+1} = \Delta_U^s$  for any s < n. Likewise, if  $\hat{c} \leq \underline{c}$ , then  $\Delta_U^s = \Delta_I = 0$  for any  $s \in \{1, ..., n\}$ , and thus  $\Delta_U^{s+1} = \Delta_U^s$  for any s < n.

We now assume  $\underline{c} < \hat{c} < P(q^C(\overline{c}))$ , and distinguish two cases.

Case 1:  $\underline{c} < \hat{c} \leq \overline{c}$ . In that case, investing allows U to become an effective supplier, and

$$\Delta_U^s = \Pi_U^s (\underline{c}) = \Pi_I (\underline{c}) - s\hat{\pi}^s (\hat{c}, \underline{c}) - (n-s)\hat{\pi}^1 (\hat{c}, \underline{c}).$$

Therefore, for  $s \in \{1, ..., n-1\}$ :

$$\begin{aligned} \Delta_U^{s+1} - \Delta_U^s &= \Pi_U^{s+1} (\underline{c}) - \Pi_U^s (\underline{c}) \\ &= -s \left[ \hat{\pi}^{s+1} (\hat{c}, \underline{c}) - \hat{\pi}^s (\hat{c}, \underline{c}) \right] - \left[ \hat{\pi}^{s+1} (\hat{c}, \underline{c}) - \hat{\pi}^1 (\hat{c}, \underline{c}) \right] \\ &\leq 0, \end{aligned}$$

where the inequality follows from the fact that retailers' outside option increases with s; this inequality is moreover strict whenever  $\hat{c} < P\left((n-s-1)q^{C}(\underline{c})\right)$ , which is the case for s large enough (since  $\hat{c} \left( < P\left(q^{C}(\overline{c})\right) \right) < P(0)$ ).

Case 2:  $(\underline{c} <) \overline{c} < \hat{c} < P(q^{C}(\overline{c}))$ . In that case, U is already an effective supplier when it faces a cost  $\overline{c}$ , and investing allows it to further increase its efficiency; we then have:

$$\Delta_U^s = \Delta_I + (n-s) \left[ \hat{\pi}^1 \left( \hat{c}, \overline{c} \right) - \hat{\pi}^1 \left( \hat{c}, \underline{c} \right) \right] + s \left[ \hat{\pi}^s \left( \hat{c}, \overline{c} \right) - \hat{\pi}^s \left( \hat{c}, \underline{c} \right) \right].$$

From Proposition 5,  $\Delta_U^n = \Delta_I$  and  $\Delta_U^s \ge \Delta_I$  for any s < n, with a strict inequality when  $\hat{c} < P((n-s)q^C(\bar{c}))$ . Therefore:

- Since  $\hat{c} < P\left(q^{C}(\overline{c})\right), \Delta_{U}^{n-1} > \Delta_{U}^{n} = \Delta_{I}$ ; therefore, there exists  $\overline{s} \leq n$  such that  $\Delta_{U}^{s-1} > \Delta_{U}^{s}$  for  $s \in \{\overline{s}, ..., n\}$ .
- If in addition  $\hat{c} \geq P\left((n-1)q^{C}(\bar{c})\right)$ , then  $\Delta_{U}^{s} = \Delta_{I}$  for s small enough (namely, as long as  $\hat{c} \geq P\left((n-s)q^{C}(\bar{c})\right)$ ), whereas  $\Delta_{U}^{s} > \Delta_{I}$  for s large enough (e.g., for s = n-1); therefore, there exists  $\underline{s} \geq 1$  such that  $\Delta_{U}^{s+1} \geq \Delta_{U}^{s}$ , with at least one strict inequality, for  $s \in \{1, ..., \underline{s}\}$ .

### F.2 Illustration: linear demand

Suppose that demand is linear: P(Q) = 1 - Q. We then have:

•  $q^{C}(c)$  solves

$$\arg\max_{q} \left( P\left( (n-1)q^{C}(c) + q \right) - c \right) q = \left( 1 - (n-1)q^{C}(c) - q - c \right) q,$$

and is thus characterized by the first-order condition

$$0 = \left(1 - (n-1)q^{C}(c) - q - c\right)q\Big|_{q=q^{C}} = 1 - c - (n+1)q^{C}(c) = 0,$$

i.e.

$$q^{C}\left(c\right) = \frac{1-c}{n+1}.$$

• A member of a group of size *s* obtains

$$\hat{\pi}^{s} = \left(\hat{P}\left((n-s)\,q^{C} + (s-1)\,\hat{q}^{s} + \hat{q}^{s}\right) - \hat{c}\right)\hat{q}^{s} \equiv \max_{q}\left(\hat{P}\left((n-s)\,q^{C} + (s-1)\,\hat{q}^{s} + q\right) - \hat{c}\right)q$$

where

$$\left(\hat{P}\left((n-s)\,q^{C}+(s-1)\,\hat{q}^{s}+q\right)-\hat{c}\right)q = \left(1-(n-s)\,q^{C}-(s-1)\,\hat{q}^{s}-q-\hat{c}\right)\hat{q}$$

The first-order condition yields, for  $q = \hat{q}^s$ :

$$0 = 1 - (n - s) q^{C}(c) - s\hat{q}^{s} - \hat{c} - \hat{q}^{s} = 1 - (n - s) q^{C}(c) - (s + 1) \hat{q}^{s} - \hat{c},$$

or

$$(s+1)\,\hat{q}^s + (n-s)\,\frac{1-c}{n+1} = 1 - \hat{c},$$

leading to:

$$\hat{q}^{s}(\hat{c},c) = \frac{(s+1) - (n+1)\hat{c} + (n-s)c}{(n+1)(s+1)},$$
  
$$\hat{\pi}^{s}(\hat{c},c) = \left(\frac{(s+1) - (n+1)\hat{c} + (n-s)c}{(n+1)(s+1)}\right)^{2}.$$

Therefore,  $\hat{q}^{s}(\hat{c},c)$  and  $\hat{\pi}^{s}(\hat{c},c)$  are positive if and only if

$$s > \hat{s}(c) = \frac{(n+1)\hat{c} - 1 - nc}{1 - c}.$$

We then have  $\bar{s} = \hat{s}(\bar{c})$  and  $\underline{s} = \hat{s}(\underline{c})$ .

In particular, for n = 10 and  $\hat{c} = 0.7$ , we have:

$$\hat{s} = \left[\frac{(10+1)\,\hat{c} - 1 - 10c}{(1-c)}\right]_{\hat{c}=0.7} = \frac{10c - 6.7}{c - 1},$$

Thus, for  $\bar{c} = 0.45$  and  $\underline{c} = 0$ :  $\bar{s} = \left[\frac{10c-6.7}{c-1}\right]_{c=0.45} = 4$  and  $\underline{s} = \left[\frac{10c-6.7}{c-1}\right]_{c=0} = 6.7$ , and

$$\hat{\pi}^{s}(\hat{c},\bar{c}) = \left[ \left( \frac{(s+1) - (n+1)\hat{c} + (n-s)\bar{c}}{(n+1)(s+1)} \right)^{2} \right]_{n=10,\hat{c}=0.7,\bar{c}=0.45} = \frac{1}{121} \frac{(0.55s - 2.2)^{2}}{(s+1)^{2}},$$
$$\hat{\pi}^{s}(\hat{c},\underline{c}) = \left[ \left( \frac{(s+1) - (n+1)\hat{c} + (n-s)\underline{c}}{(n+1)(s+1)} \right)^{2} \right]_{n=10,\hat{c}=0.7,\underline{c}=0} = \frac{1}{121} \frac{(s-6.7)^{2}}{(s+1)^{2}},$$

which was used to generate Figure 1.a.

Turning to investment incentives, we have

$$\Pi^{C}(c) = n\hat{\pi}^{1}(c,c) = \frac{10}{121}(1-c)^{2},$$

and thus:

$$\Delta_I = \Pi^C(\underline{c}) - \Pi^C(\overline{c}) = \left[\frac{10}{121} \left(1 - c\right)^2\right]_{c=0} - \left[\frac{10}{121} \left(1 - c\right)^2\right]_{c=0.45} = 5.7645 \times 10^{-2}.$$

Using  $\Delta_U^s = \Delta_I + s \left[ \hat{\pi}^s \left( \hat{c}, \overline{c} \right) - \hat{\pi}^s \left( \hat{c}, \underline{c} \right) \right]$  leads to:

- For s = 1, ..., 4,  $\hat{\pi}^s(\hat{c}, \overline{c}) = \hat{\pi}^s(\hat{c}, \underline{c}) = 0$  and thus  $\Delta_U^s = \Delta_I$ .
- For  $s = 5, 6, \hat{\pi}^s(\hat{c}, \overline{c}) > \hat{\pi}^s(\hat{c}, \underline{c}) = 0$  and thus U's bias is positive:

$$\Delta_U^s - \Delta_I = s\hat{\pi}^s \left(\hat{c}, \overline{c}\right) = s \frac{1}{121} \frac{\left(0.55s - 2.2\right)^2}{\left(s+1\right)^2} > 0,$$

and increases with s.

• For  $s = 7, ..., 9, \hat{\pi}^s(\hat{c}, \overline{c}) > \hat{\pi}^s(\hat{c}, \underline{c}) > 0$  and thus U's bias remains positive:

$$\Delta_U^s - \Delta_I = s \left[ \hat{\pi}^s \left( \hat{c}, \overline{c} \right) - \hat{\pi}^s \left( \hat{c}, \underline{c} \right) \right] = s \left[ \frac{1}{121} \frac{\left( 0.55s - 2.2 \right)^2}{\left( s + 1 \right)^2} - \frac{1}{121} \frac{\left( s - 6.7 \right)^2}{\left( s + 1 \right)^2} \right] > 0,$$

but decreases as s increases, as illustrated by Figure 1.b.

• Finally, for s = 10,  $\hat{\pi}^s(\hat{c}, \overline{c}) = \hat{\pi}^s(\hat{c}, \underline{c}) > 0$ , and thus again  $\Delta_U^s = \Delta_I$ .